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## **John Dominy school exercise book [newspaper, The Spectator, March 18, 1801, used as covers] : surveying. 1810**

Dominy, John

[s.l.]: [s.n.], 1810

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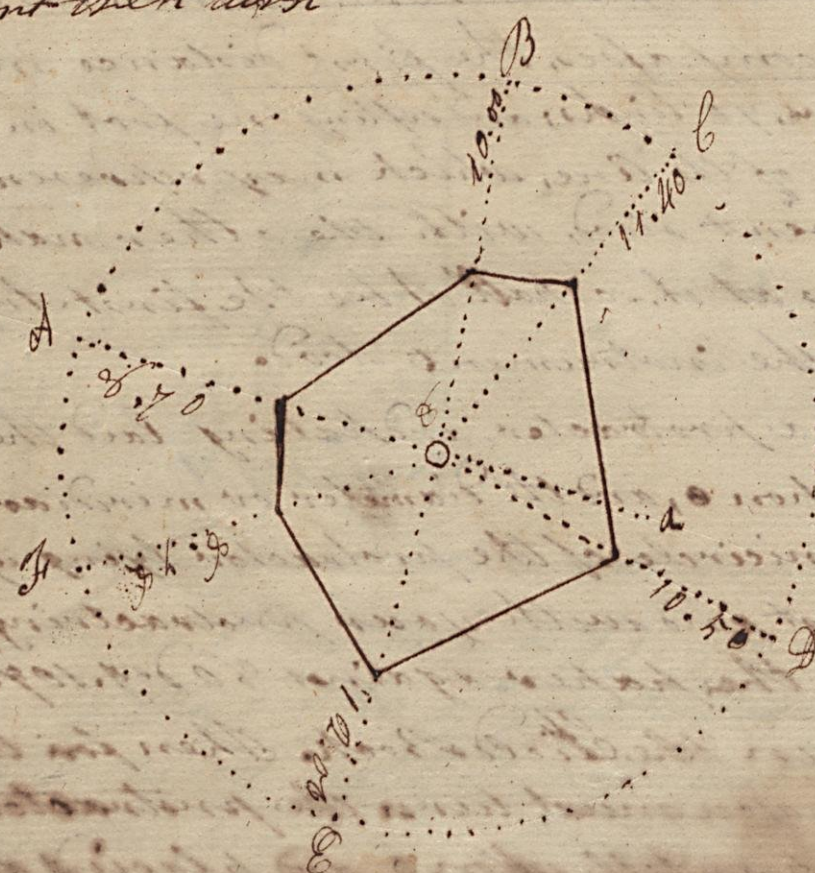


John Dominy,

# (1) Surveying. July 28<sup>th</sup> 1810.

To take the Plot of a field at one station in any place to-  
 wit, from whence you can see all the angles by the semi-  
 circle.

Admit  $ABCD E F$  to represent a field, of which you are to  
 take a plot first set your semicircle upon the staff at any  
 convenient place thereof as at  $O$ , and cause marks to be set up  
 in every angle: direct your instrument, the flower de luce being  
 from you, to any one angle: as for example to  $A$ ; and copying  
 the mark at  $A$  through the fixed sights screw fast the  
 instrument then turn



the immovable index about (the semi-circle remaining  
 immovable) till through the sights thereof you copy the mark  
 at  $B$ . See what degrees on the brass limb are cut by the  
 index which suppose  $60$ ; write that down in your field  
 book; so turn the index round to every one of the other  
 angles putting down in your field book what degree the  
 index points to. As for example at  $C$   $109$  degrees, at  $D$   $116$ ,  
 but at  $E$ , the end of the index will go of the brass limb, so  
 the other end will come on, you must then find out  
 what degrees the index cut in the  
 limb at  $E$  which is  $100$ ; suppose  $100$  degrees at  $F$ .

Plotting Continued July 30<sup>th</sup> 1810

These observations you must note down in your field-book thus

| Angles | Degrees | Minutes | Chains | Links |
|--------|---------|---------|--------|-------|
| o A    | 000     | 00      | 8      | 40    |
| o B    | 090     | 00      | 10     | 00    |
| o C    | 107     | 00      | 11     | 40    |
| o D    | 155     | 00      | 10     | 50    |
| o E    | 260     | 00      | 12     | 00    |
| o F    | 315     | 00      | 8      | 48    |

To protract the former Observations taken.

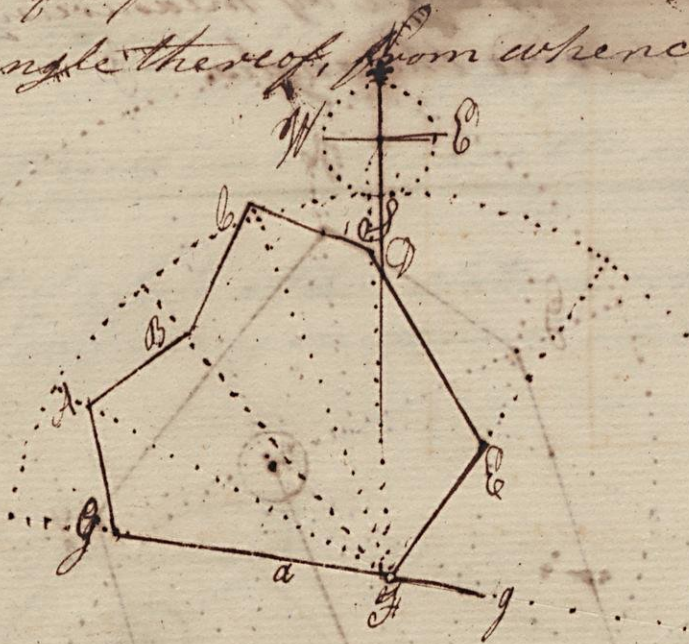
First draw a line at pleasure as *o a*; then take from your scale with your compasses, the first distance measured, viz. from *o* to *A*, 8 chains, 40 links; and setting one foot in any any convenient place of the line, which may represent the place where the instrument stood, with the other make a mark upon the line as *at a*, so that *A* be the first angle, and *o* the place where the instrument stood.

Secondly, take a protractor, and having laid the center hereof exactly upon *o*, and the diameter or meridian upon the line *o a*, the semicircle of the protractor lying upwards; then hold it fast and with your protracting pen make a mark upon the paper against 90 deg. 107 deg. &c. as you find them in the Field Book. Then for those degrees that exceed 90, you must turn the protractor downward keeping the center still upon *o*, and placing again the diameter upon *o a*. Mark out by the innermost circle of divisions the rest of your observations 155, 260, 315. Then applying a scale to *o* and every one of the marks, draw the dotted lines *o B*, *o C*, *o D*, *o E*, *o F*.

Thirdly, take with your compasses the length of the line *o B*, which you find by the field-book to be 10 chains, which set off from *o* to *B*. The like to do for *o C*, *o D*, and the rest. Lastly, draw the lines *A B*, *B C*, *C D*, &c. which will inclose a figure exactly proportionable to the field before surveyed.

# Plotting Continued. <sup>3</sup>

To take the plot of a field at one station by the semicircle placed in any angle thereof, from whence the other angles can be seen.



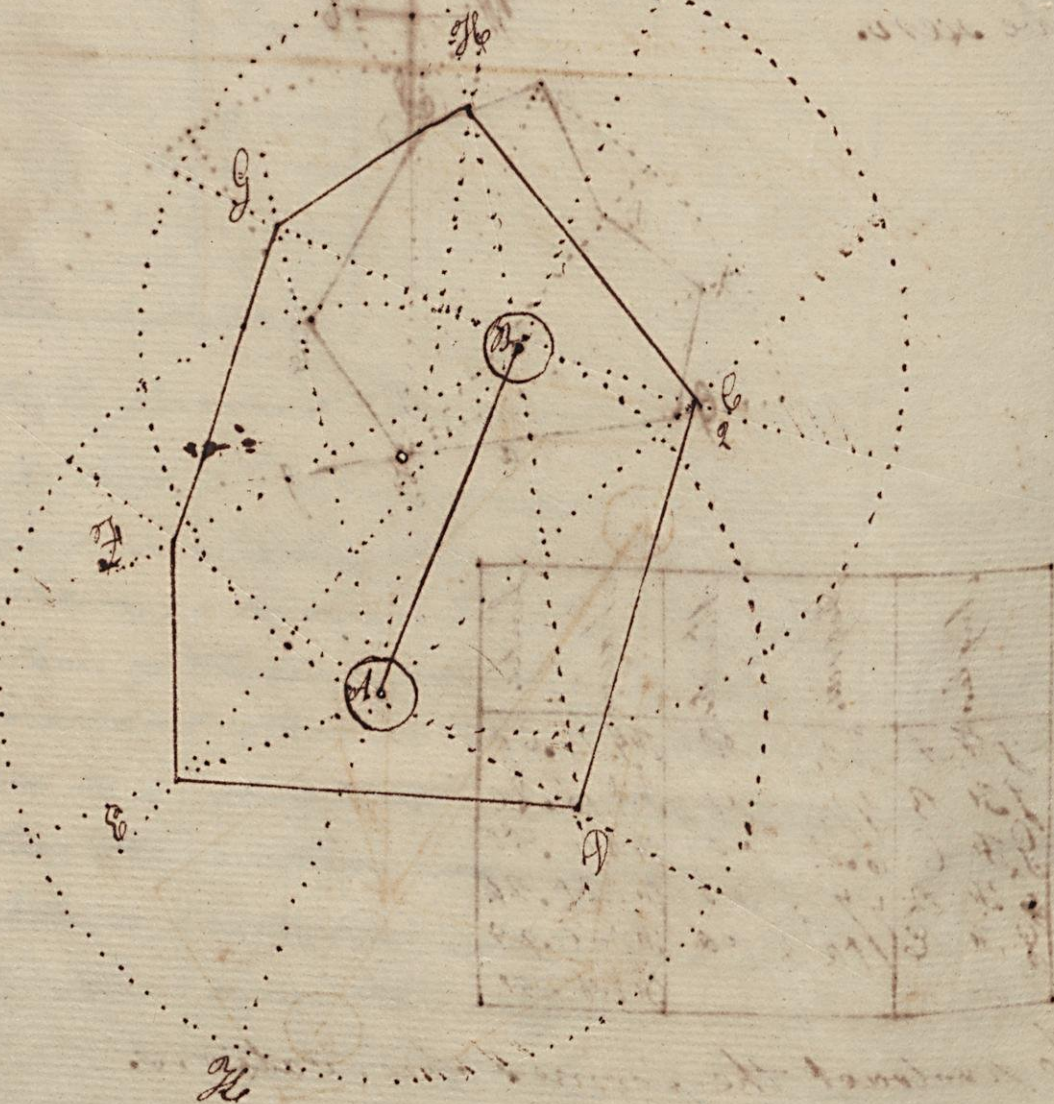
| Angles. | Degrees. | Minutes. | Chains. | Links. |
|---------|----------|----------|---------|--------|
| Ih A    | 20.      | 00       | Ih 14.  | 60     |
| Ih B    | 40.      | 00       | Ih 18.  | 20     |
| Ih C    | 60.      | 00       | Ih 16.  | 50     |
| Ih D    | 77.      | 00       | Ih 21.  | 20     |
| Ih E    | 110.     | 00       | Ih 16.  | 99     |
| Ih      |          |          | Ih 8.   | 51     |

To protract the former observations.

Draw a line at adventure as Ig, upon any convenient place on which lay the center of your protractor as at I, keeping the diameter thereof right upon the line Ig. Then make marks round the protractor at every angle as you find them in the field book viz. against 20, 40, 60, 77, and 110; which done take away the protractor, and applying the scale or ruler to I, and each of the marks, draw the lines Ih, IA, IB, IC, ID, and IE. Then setting off upon these lines the true distances as you find them in the field book thus for the first line Ih, 14 chains, 60 links; for the second Ih 18 chains, 20 links &c. make marks where the end of these distances fall, which let be at G, A, B, C, &c. Lastly, Between these marks, drawing the lines G, A, B, C, D, E, &c. I, G, you will have completed the work.

Continued, July 31<sup>st</sup> 1810.

To take the plot of a field at two stations provided from either station you can see every angle by measuring only the stationary distance, and observed the angles.



Angles. Degr Min.

B A C — 24 — 30

B A D — 94 — 00

E — 225 — 00

F — 283 — 30

G — 325 — 00

H — 346 — 00

First station.

Angles. Degr Min.

I B C — 84 — 00

I B D — 1149 — 00

E — 194 — 00

F — 215 — 00

G — 240 — 00

H — 322 — 00

Second Station.

How to protract or lay down upon paper these following observations.

First, draw a line cross your paper at pleasure, as the line  $I A$  and set it upon that line, as from  $A$  to  $B$  so shall  $A$  represent the first station,  $B$  the second.

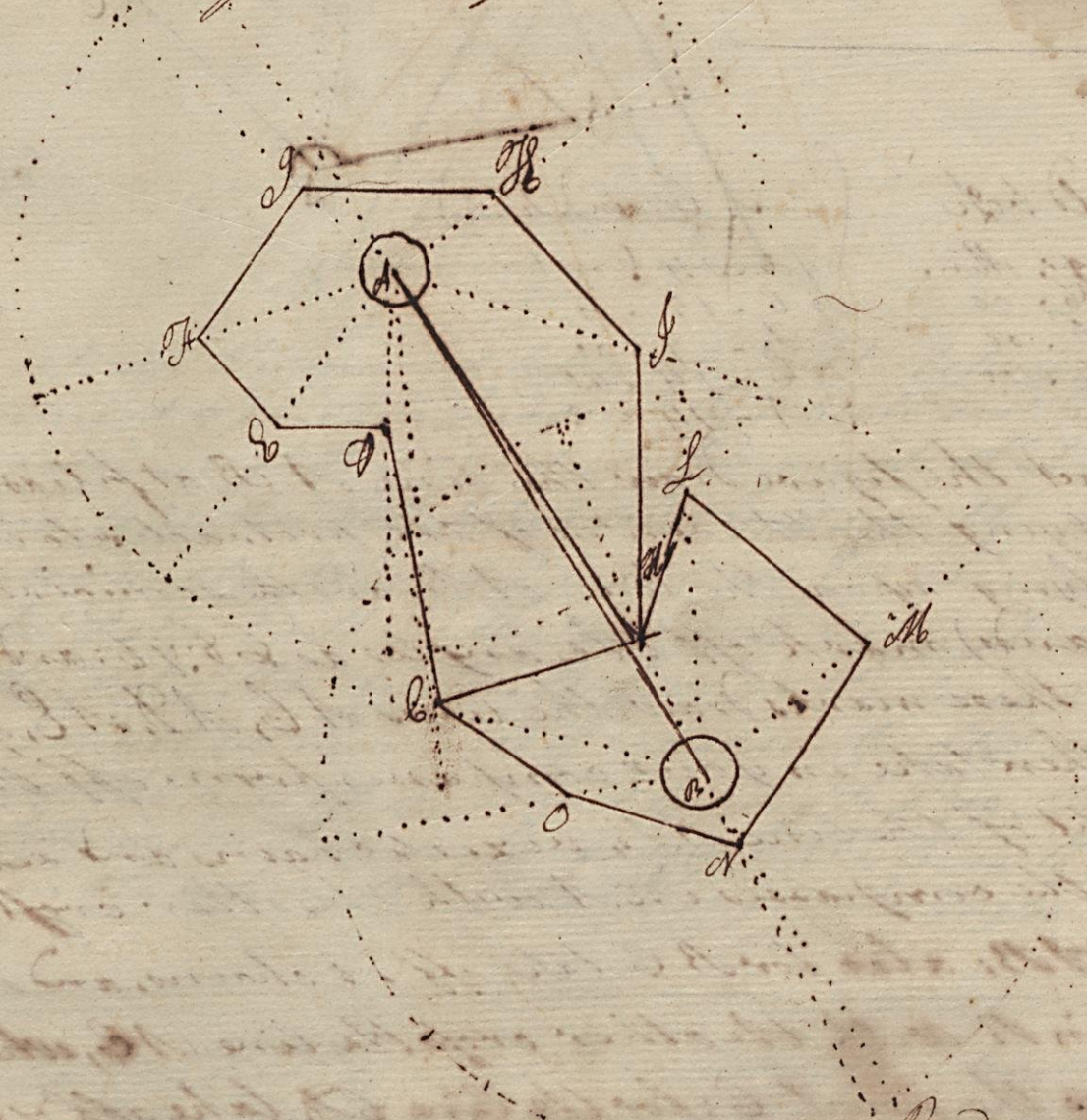
Secondly, Apply the center of your protractor to the point  $A$  the diameter lying straight upon the line  $A B$ ; mark it the angle, as you find them in your field book through those marks from  $A$  draw lines of conver



Plotting Continued. August 1<sup>st</sup> 1810.

Thirdly, Move your protractor to the second station B; and there mark out your angles, and draw lines as before, at the first station. Lastly, The places where the lines of the first station, and the lines of the second intersect each other are the angles of the field.

To take the Plot of a field at two stations, when the field is so irregular that from one you cannot see all the angles,



First Station

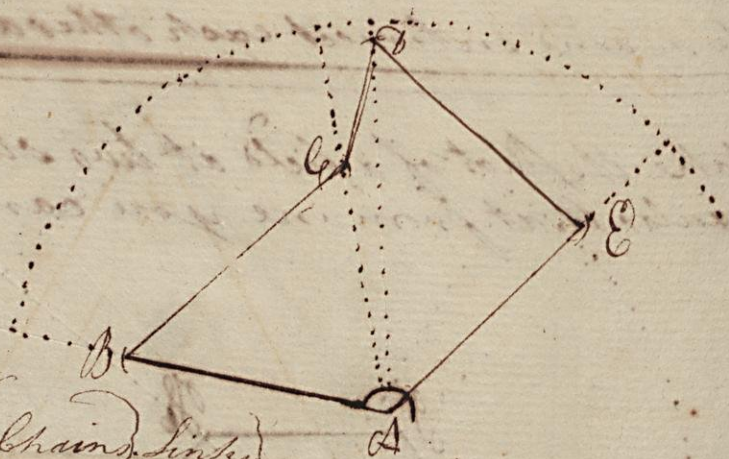
Second Station

| Angles, Degrs. Min. | Chains, Links. | Angles, Degrs. Min.   | Chains, Links. |
|---------------------|----------------|-----------------------|----------------|
| C A D - 25 - 00     | 20 : 45        | B B N - 3 - 30 - 4    | 29             |
| C A E - 26 - 00     | 8 : 10         | B B O - 111 - 00 - 4  | 00             |
| C A F - 34 - 00     | 9 : 55         | B B G - 145 - 00 - 15 | 60             |
| C A G - 104 - 00    | 10 : 50        | H - 202 - 00 - 7      | 48             |
| H - 137 - 00        | 7 : 00         | L - 217 - 00 - 15     | 00             |
| D - 262 - 00        | 6 : 40         | M - 271 - 00 - 18     | 20             |
| H - 316 - 00        | 13 : 40        |                       |                |
| K - 354 - 00        | 24 : 40        |                       |                |

John Dominy, East Hampton, 1810

Plot Continued. August 2<sup>d</sup> 1810.

To take the plot of a field at one station in an angle (protract) that from that angle you can see all the other angles (by measuring round about the said field).



| Field base        | (Links) | (Chains) | (Links) |
|-------------------|---------|----------|---------|
| Angles. Deg. Min. | AB      | 14       | 00      |
| BAC - 66.00       | BC      | 15       | 00      |
| BAD - 76.00       | CD      | 7        | 00      |
| BAE - 124.00      | DE      | 14       | 40      |
|                   | EA      | 14       | 5       |

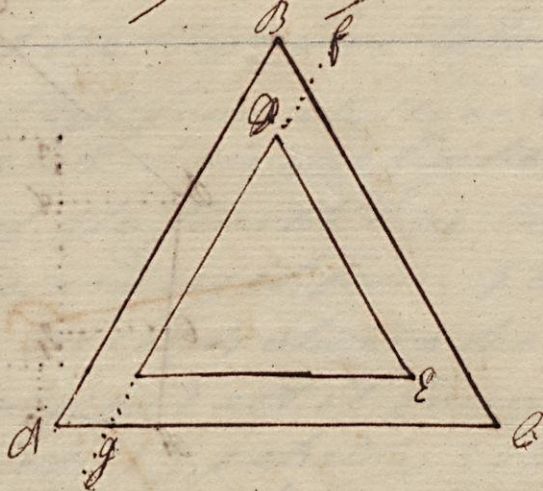
To protract the figure draw the line AB at pleasure; and applying the the centers of the protractor to A (the diameter lying upon the line AB, and the semicircle of it upwards) mark off the angles as  $\angle BAC$ : 66: and  $\angle BAD$ : through these marks draw the lines AC, AD, AE, of sufficient length. Then take in your compasses from off the scale the length of the line AB, viz. 14 chains and setting one foot of the compasses in A with the other cross the line as at B; also for BC take off 15 chains, and setting one foot in B with the other cross the line AC, which determines the point C; for the line CD, take off 7 chains, and setting one foot in C, cross the line AD, at D; then for DE, take 14 chains, 40 links, and setting one foot of the compasses in D, with the other foot cross the line AE in E. Lastly take EA 14 chains 5 links in your compasses and set one point in E, then if the other will fall upon A, you have done the work truly; if not you have erred; between the points of intersect draw straight lines, which shall be the bounds of the field, viz. AB, BC, CD, DE, EA.

John

Plot Continued. August 2 1810

Directions to measure parallel with a hedge, (when you cannot go into the hedge itself;) and also in such a case, how to take your angles.

Suppose  $ABC$  to be a field, and for the Buses, you cannot come nigher than  $c$  to plant your instrument. Let him



that sets up the marks take the Dist. between the instrument  $c$  and the hedge at  $B$ ; which Dist. let him set off again nigh  $B$ , and set up his mark at  $D$ ; likewise let him take the Dist. between the  $c$  and the hedge at  $C$ , and accordingly set up his marks at  $E$ . Then taking the angle  $DCE$ , it will be the same as the angle  $BCA$ ; so go for the rest of the Angles. But when the lines are measured

they must be measured of the same length as the outside lines, as the line  $gd$  measured from  $g$  to  $f$ , &c. The best way, therefore, is for those who measure the lines to go round the ~~field~~ on the outside thereof although the angles be taken within.

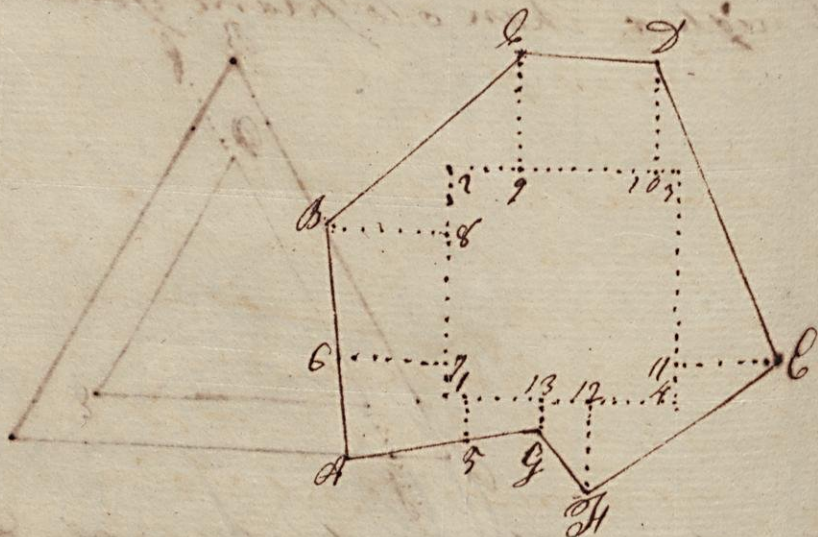
To take the plot of a field or wood, by Observing near every angle and measuring the Dist. between the marks of observation, by taking in of every line, two offsets to the hedge



East Hampton. August 13

Plotting (8) Continued. August 3<sup>d</sup> 1810.

This way of surveying is made easier (though I cannot say truer) by taking only a great square in the field, from the sides of which the off-sets are taken.



The angles 4 right angles.

The sides 12 chains, 00 links each.

I went round cum Solis, on the hedges being on my left hand.

|               |       |                       |       |
|---------------|-------|-----------------------|-------|
|               | b. L. |                       | b. L. |
| In the first  | 1 50  | Offset to a side line | 5 40  |
| line, at      | 4 30  | Offset to an angle    | 6 00  |
|               |       |                       | <hr/> |
| In the second | 3 50  | Offset to an angle    | 6 00  |
| line, at      | 10 70 | Offset to an angle    | 5 50  |
|               |       |                       | <hr/> |

|              |       |                    |       |
|--------------|-------|--------------------|-------|
| In the third | b. L. |                    | b. L. |
| line, at     | 10 00 | Offset to an angle | 5 30  |
|              |       |                    | <hr/> |

|               |       |                     |       |
|---------------|-------|---------------------|-------|
| In the fourth | b. L. |                     | b. L. |
| line, at      | 4 33  | Offset to an angle  | 4 40  |
|               | 6 70  | Offsets on an angle | 1 50  |
|               | 10 80 | Offset to a side    | 2 20  |
|               |       |                     | <hr/> |

Now to lay down upon paper the foregoing work make first a square figure as 12 34 whose side may be 12 chains. Then considering you went with the sun take 12 for the first line and taking from your scale 1 chain 50 links set it upon the line from 1 to 4; at 4 raise a perpendicular as 40, making for the second offset upon the same line take from your scale 6 chains 70 links which set upon the line from 1 to 8, and upon 8 make the perpendicular line 6 20, and so on in length.

(97)

Plotting Continued. August 4<sup>th</sup> 1810.

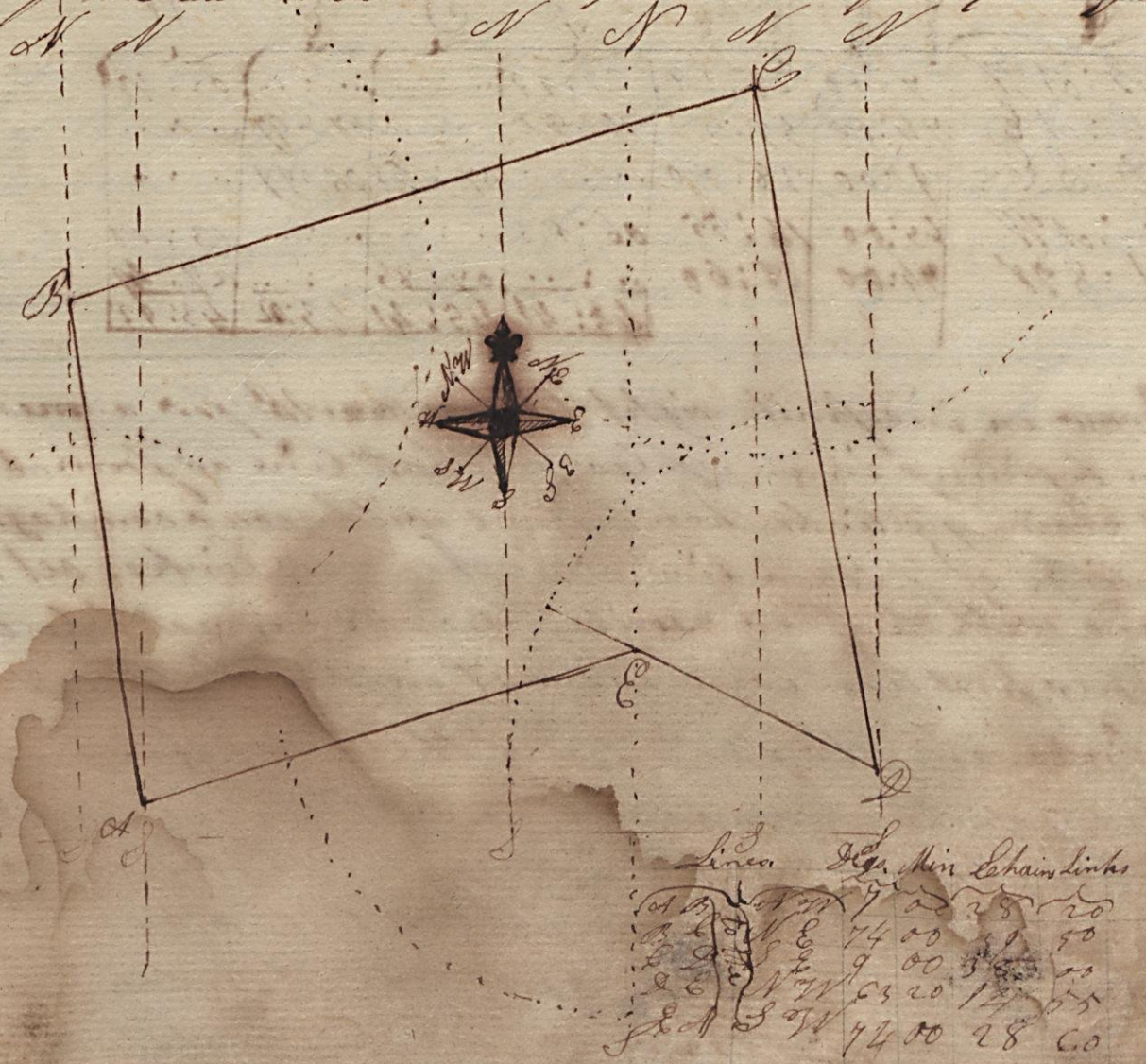
For the offsets of the second line, take 3 chains 50 links from the scale and set it from 2 to 9; at 9 make a perpendicular line 6 chains long viz. 9 6; also for the second offset of the same line, take 10 chains 40 links, and set it from 2 to 10; at 10 make the perpendicular 10 A, 5 chains 50 links in length.

For the offsets of the third line take from your scale 10 chains, and set it up from 3 to 11; and at 11 make the perpendicular 11 E, 5 chains, 30 links long.

For the offsets of the fourth line take from your scale 4 chains 30 links, and set it from 4 to 12; and at 12 make the perpendicular 12 A, 4 chains 40 links long. Also take 6 chains 40 links and set it from 4 to 13; and at 13 make the perpendicular 13 G, 1 chain, 50 links long.

Lastly, take 10 chains, 80 links and set it from 4 to 1; and at 1, make the perpendicular 1, 5, 2 chains 20 links long.

By the help of the needle to take the plot of a large wood; by going round the same, and making use of that division of the card that is numbered with four 90° or quadrants.



(10)

# Plotting Continued.

August 6<sup>th</sup> 1810.

To lay down which upon paper, draw parallel lines as *AB*, *BC*, &c. to represent meridians or north and south lines, then applying the protractor (which should be graduated accordingly with twice 90 degrees, beginning at each end of the diameter, and meeting in the middle of the arch) to any convenient place of one of the lines as to *A*, lay the meridian line of the protractor to the meridian line on the paper, and against 7 degr. make a mark through which draw a line and set off thereon the dist. *AB* 28 chains 20 links. Secondly, apply the center to the protractor to *B*, and turning the semicircle thereof the other way, because you see the course tends to the eastward, make the diameter thereof lie parallel to the meridian lines on the paper (which you may do by the figure, at the ends of the parallelogram) and against 7 1/2 degrees make a mark and set off 39 chains 50 links and draw the line *BC*; and the like do by the other lines and angles until you come round to the place where you began.

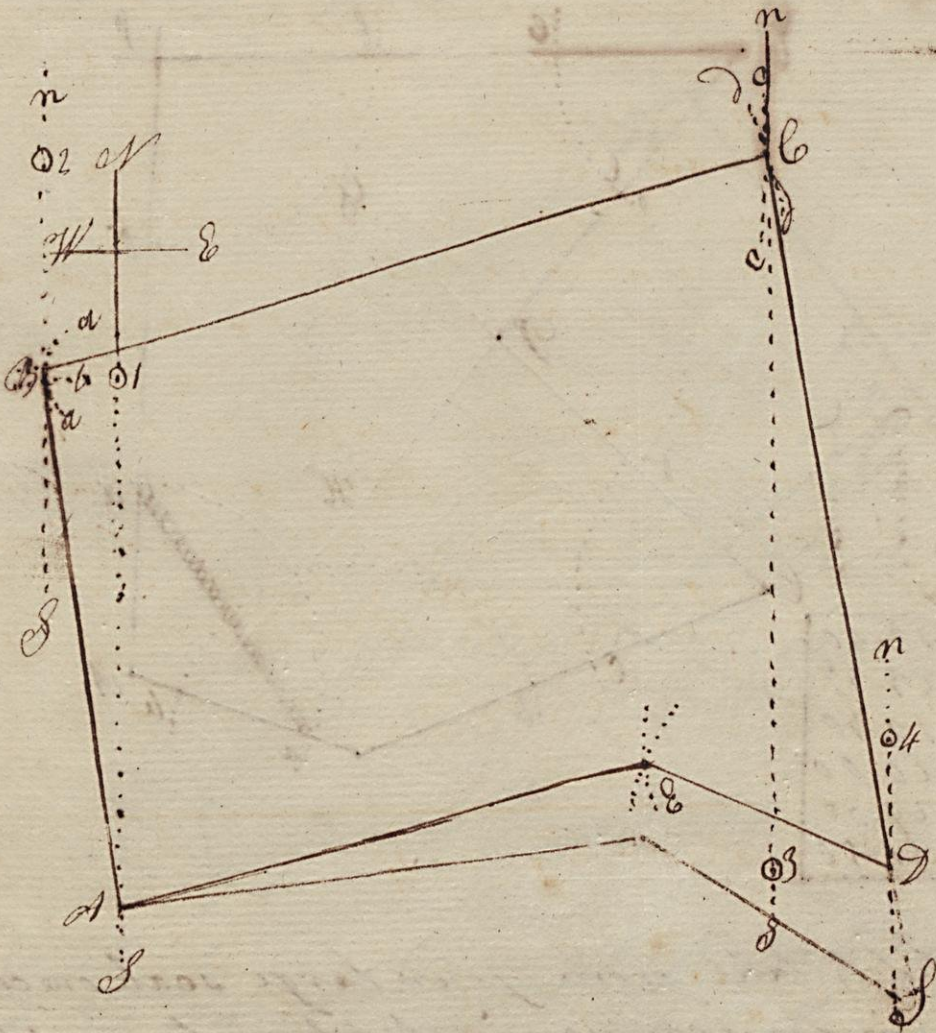
The same <sup>done</sup> in another manner,

|                       | Degrees. | Minutes. | Seconds. | N     | S     | E     | W     |
|-----------------------|----------|----------|----------|-------|-------|-------|-------|
| <i>AB</i> : <i>NW</i> | 4:00     | 28:20    |          | 27:99 | ...   | ...   | 03:43 |
| <i>BC</i> : <i>NE</i> | 44:00    | 39:50    |          | 10:46 | ...   | 37:97 | ...   |
| <i>CD</i> : <i>SE</i> | 9:00     | 38:00    |          | ...   | 37:58 | 05:99 | ...   |
| <i>DE</i> : <i>NW</i> | 45:00    | 14:57    |          | 06:53 | ...   | ...   | 13:00 |
| <i>EA</i> : <i>SW</i> | 44:00    | 28:60    |          | ...   | 04:88 | ...   | 27:49 |
|                       |          |          |          | 45:41 | 45:41 | 43:02 | 43:92 |

Draw an indefinite right line as *no* *AB* for a meridian line; then beginning in any place of that line as from *A* to *C* 1. viz. 27 chains 99 links then taking with your compasses the westings of the same line viz. 18 chains 43 links; set one foot in *C*, and with the other describe the arch *a*; next take the length of your first line as you find it in the field book, viz. 28 chains 20 links, and setting one foot of the compasses in *A*, with the other cross the former arch *a* with another arch *B*, and in *B* the intersection of the arches is your second angle. Then through *B* draw another north and south line as *BC*, parallel to the first *no* *AB*; then take <sup>with</sup> your compasses the northing of the second line viz. 10 chains 89 links, and set it upon that line, from *B* to *C*; take

(11)

Plotting Continued. August 6<sup>th</sup> 1810.

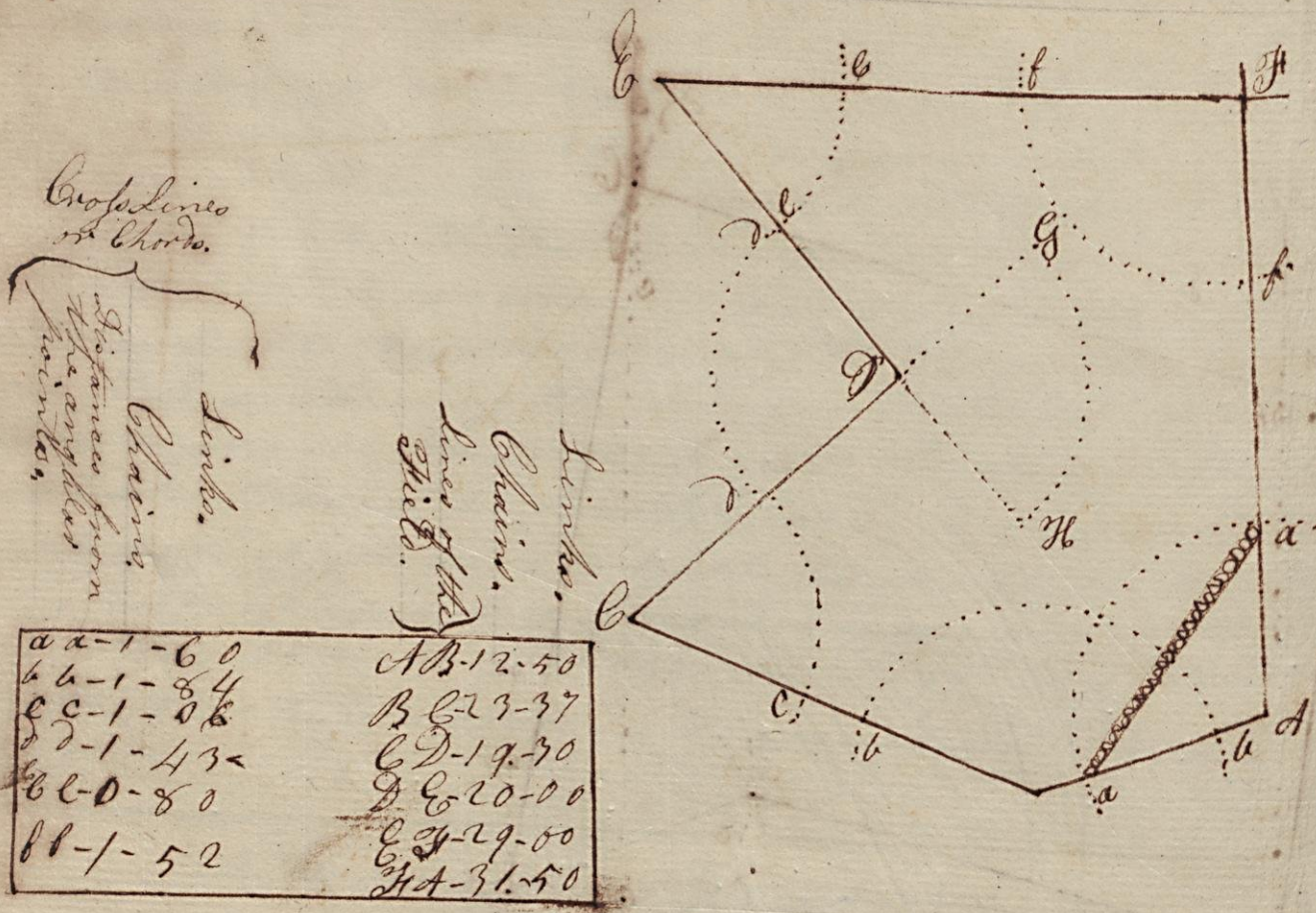


casting of the same line viz. 37 chains, 97 links; and setting one foot of the compasses in o2, with the other sweep the arch oc; and also take with your compasses the length of the second line viz. 39 chains, 50 links, and setting one foot in B, cross the former arch with another ~~arc~~; the intersection C is your third angle.

To survey a field with the chain only by going round the inside of it.

Plotting Continued. (12) August 7<sup>th</sup> 1810.

To survey a field with the chain only, by going round the inside of it.



Cross lines  
or Chords.  
Distances from  
the angles  
links.  
Chaining  
links.

links.  
Chaining  
links.  
line of the  
field.

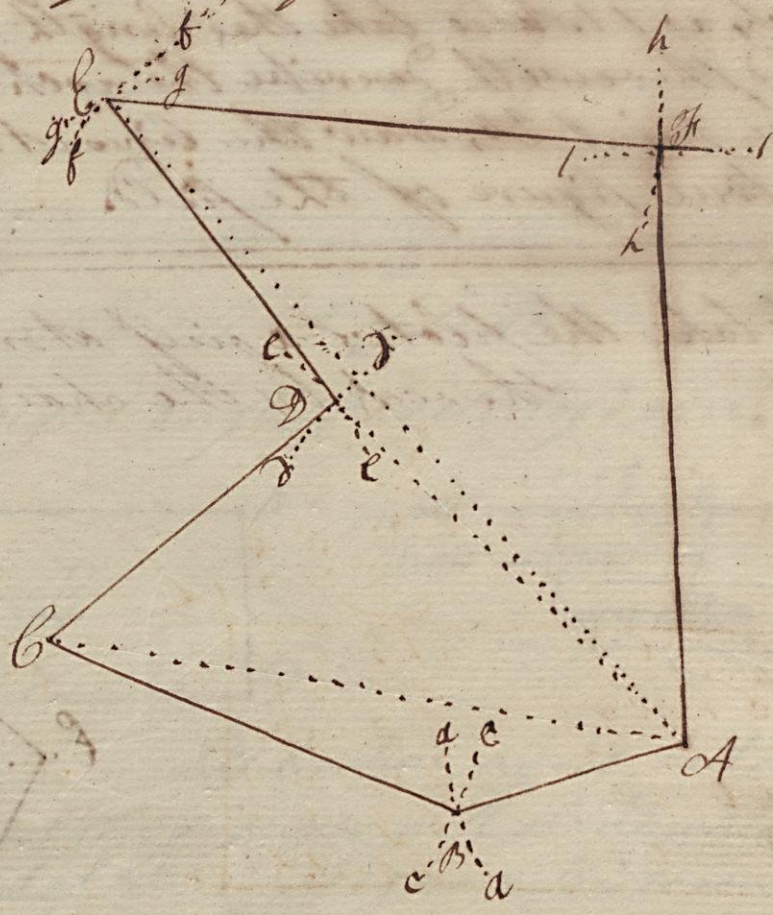
Now to begin to plot, take from your large scale one chain, with that distance, in any convenient place of your paper; as at *aa*, sweep the arch *aa*; then from the same scale take off 1 chain 60 links and set it upon that arch, as from *a* to *a'*; and draw through the point, *a* and *a'*, the right line *AB*, *AF*; then repairing to your shorter scale, take from them the first distance, viz. 12 chains, 50 links; and setting it from *A* to *B*, draw the line *AB*.

Secondly, Repairing to *B*, take from your large scale one chain, and setting one foot of the compasses in *B* with the other describe the arch *bb*; also from the same scale take your chord line viz. 1 chain 84 links and set it upon the arch *bb*, having one foot of the compasses in the point where the arch intersects *AB*, the other will fall at *b*; then through *b* draw the line *BC*; and from your smaller scale set off the distance 23 chains 37 links from *B* to *C*, where the next angle is made; after this manner proceed according to your field book till you have done.



Plotting Continued (13) August 4<sup>th</sup> 1810

The common way taught by surveyors for taking the plot of the foregoing, or any other field.



Chains.  
Links.

AC 33 40  
AD 25 40  
AE 45 40

Take a plot which, first draw a right line AC at pleasure, and set off thereon 33 chains 40 links according to your field-book for the first diagonal, then taking with your compasses the length of the line AB, viz. 12 chains 50 links, and setting one foot in A with the other describe the Arch aa; also take the line BC, viz. 23 chains 37 links, and setting one foot in C, with the other describe the Arch cc, cutting the Arch aa, in the point B; then draw the lines AB, CB, which shall be the two bound-lines of the field.

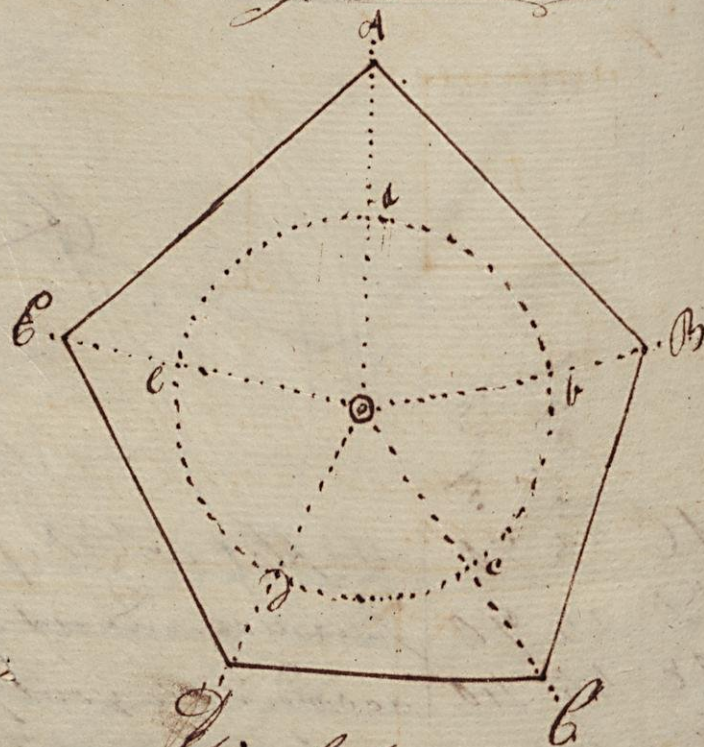
Secondly, Take with your compasses the length of the diagonal AD, viz. 25 chains 40 links and setting one foot of the compasses in A, with the other describe the arch dd; also taking the line CD, viz. 19 chains, 30 links, set one foot in C, and with the other describe the arch ee, cutting the arch dd in the point D, to this intersection draw the line CD.

Thirdly, Take with your compasses the length of the diagonal AE, viz. 45 chains, 40 links; and setting one foot in A, with the other describe an arch as ff; also take the line DE, 20 chains and therewith cross the former arch in the point E, and draw the line DE.

Plotting Continued (14)  
 August 6<sup>th</sup> 1810.

Lastly, Take with your compasses the length of the line AB, viz. 51 chains, 50 links; and setting one foot in ch. describe an arch, as 11. Also take the length of the line EF viz. 29 chains, and therewith describe the arch hh, to cut the arch 11 in the point H; draw the lines AH and EH, and you will have a true figure of the field.

To take the plot of a field at one station near the middle thereof by the chain only.



|                              | Ch. Link. |                              | Chain Link  |
|------------------------------|-----------|------------------------------|-------------|
| Subtending<br>or chord lines | ab 1.26   | Diagonal<br>or center lines. | o A. 18. 10 |
|                              | bc 1.06   |                              | o B. 15. 00 |
|                              | cd 1.00   |                              | o C. 17. 00 |
|                              | de 1.20   |                              | o D. 15. 00 |
|                              |           |                              | o E. 16. 00 |

To plot the field by these observations.

Take from a large scale 1 chain, and setting one foot of the compasses in any convenient place of the Paper as at o, make the circle a b c d e; then taking for your first subtendent, or chord line 1 chain, 26 links, set it upon the circle, as from a to b. From o through a and b draw lines, as o a o b, which produce as far as may be convenient. Then take your links, and set it upon the circle from b to c and draw the line o c. When you have thus set off all your subtendents, and drawn lines through their several marks, take a smaller scale, and upon all the lines a b c d e draw,

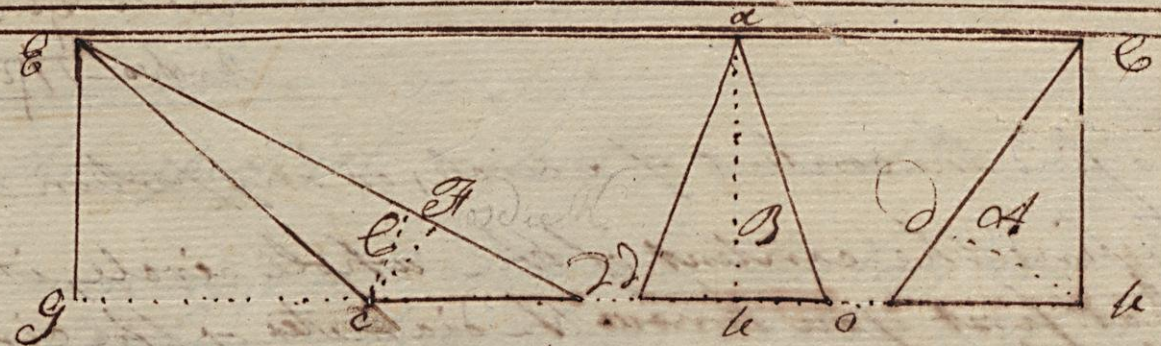
set off the diagonal or center lines as you find them in the field-book: thus upon the line  $ca$  set off 18 chains, 10 links, from  $c$  to  $A$ ; upon the line  $cb$ , 15 chains from  $c$  to  $B$ ; and so by all the rest. Lastly, Draw the lines  $AB$ ,  $BC$ ,  $CA$ , &c. and the work is finished.

To find the Content of a Plot of Land.  
Of the square and right angled parellelogram.



|       |    |    |    |
|-------|----|----|----|
| Acres | 20 | 40 | 00 |
|       | 20 | 60 | 00 |
| Roods | 3  | 46 | 00 |
|       | 3  | 46 | 00 |
|       | 4  | 00 | 00 |

I need not have put down the multiplication by 40; but only to show you in what order the figures will stand when you have odd perches. The content of the long square  $B$  is 20 acres 2 roods, 00 perch.



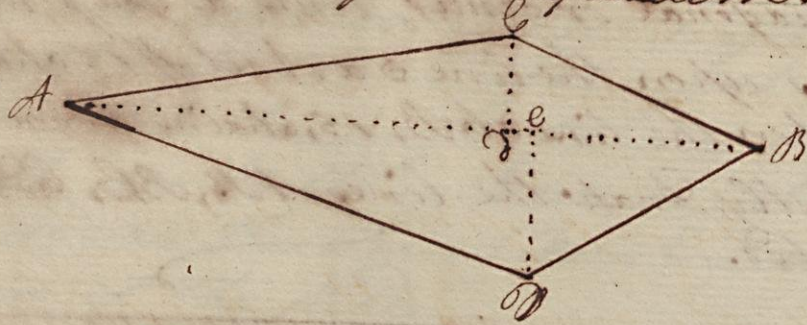
In the triangle  $A$  the base  $ab$ , is 10 chains the perpendicular or  $cb$  13 chains, 40 links the half of which is 6 chains, 40 links; which multiplied by 10 chains fait 64000; from which cutting off five figures there is left 6 Acres. Then multiplying the remainder by 4 fait 240000; from which taking 5 figures remains 3 roods. Again the 5 figures cut off multiplied by 40, makes 160000; from which taking 5 figures, leaves 16 perches. See the operation.

|         |   |   |   |    |
|---------|---|---|---|----|
|         | 6 | 4 | 9 | 00 |
| Acres   | 6 | 4 | 9 | 00 |
| Roods   | 3 | 4 | 6 | 00 |
| Perches | 1 | 6 | 0 | 00 |

(16)

To find the content *Continued*. August 9<sup>th</sup> 1810.

To find the content of a trapezium.

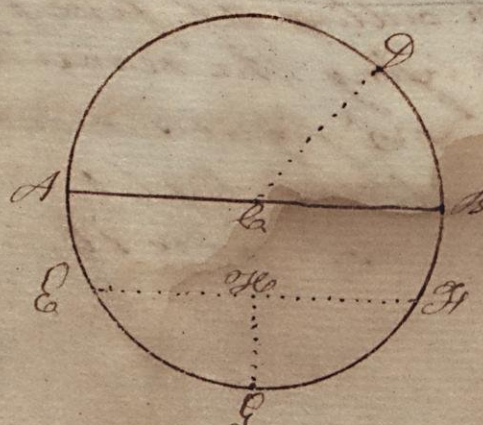


Take the length of the line A B, which let be 34 chains take also the length of the perpendicular D e, which let be 4 chains, 40 links; and also C d, 4 chains, 80 links; add the two perpendiculars together and they make 12 chains 20 links which multiply by half the common base A B, 18 chains 50 links, and the product is 22 acres 2 roods 11 perches as appears by the operation hereunder.

Half the common base A B 18.50  
 The sum of the two perpendiculars 12.20

|         |          |
|---------|----------|
|         | 37000    |
|         | 37000    |
|         | 1850     |
| Acres   | 22 59000 |
|         | 4        |
| Roods   | 2 8000   |
|         | 46       |
| Perches | 11 000   |

To find the content of a circle, or any portion thereof. To find the content of the whole circle, it is convenient that first you know the diameter or the circumference thereof; one of which being known the other is easily found, for as 4 is to 22 so is the diameter to the circumference, and as 22 is to 7 so is the circumference to the diameter.



By the diameter only to find the content. As 14 is to 14, so is the square of the diameter to the content. The square of the diameter is 40000, which multiplied

To find *Continued* August 9<sup>th</sup> 1870

by 14, makes 440000; which, divided by 14, gives 31428  
or 1 rood 14 perches, and something more for the content.

To measure the superficial content of a sector of a circle,

Multiply half the compass thereof by the semidiameter  
of the circle the product will answer your desire.

In the foregoing circle I would know the content of that  
little piece  $D C B$ ; the arch  $D B$  is  $4 \frac{1}{2}$  links  $\frac{1}{2}$ ; the half of it  
 $39 \frac{1}{4}$ ; which multiplied by 1 chain, the semidiameter gives  
 $3925$  square links, or  $6 \frac{1}{4}$  perches.

To find the content of a segment of a circle, without knowing the diameter.

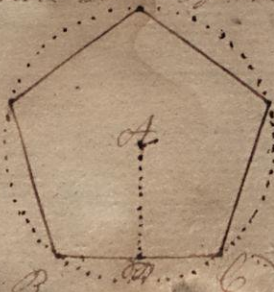
Let  $E F G$  be the segment, the chord  $E F$  is one chain 7 links  
or 170 links; the perpendicular  $G H$  50 links; now multiply  
by  $\frac{2}{3}$  of the one by the whole of the other, the product  
will be the content nearly; the  $\frac{2}{3}$  of 170 is 113, which multiplied by 50,  
produces 5650 square links, or  
9 perches.

To find the superficial content of an oval.

The common way is to multiply the long diameter by  
the shorter, and observe the content; and then as if you  
were measuring a circle, say, as 14 is to 14, so is the  
said product to the content of the oval, but this is not  
exact. A better way is, As  $1 \frac{7}{8}$  is to the length of the  
oval so is the breadth to the content, or nearer, as  $1 \frac{27}{32}$   
to the length, so is the breadth to the content.

To find the superficial content of regular polygons, pentagons, hexagons, septagons,  
Multiply half the sum of the sides by a perpendicular let fall from the center  
upon one of the sides, the product will be the area or superficial content  
of the polygon. In the following pentagon, the side  $B C$  is 84 links, the  
whole sum of the 5 sides, therefore, must be 420, the half of which is

210; which, multiplied by the perpendicular  
 $A D$ , 56 links gives 11760 square links  
for the content, or 18 perches  $\frac{2}{3}$  of  
a perch, almost 19 perches.



(18)  
Of laying out new lands.

A certain quantity of acres being given, how to lay out the same in a square figure.

Annex to the number of acres given, 5 cyphers, which will turn the acres into links; then from the number thus increased extract the square root which shall be the side of the proposed square.

Example.

Suppose the number given be 100 acres, which I am to lay out in a square figure, I join to the 100, 5 cyphers and then it is 100,0000 square links; the root of which is 1000 nearest, or 31 chains 62 links the length of one side of the square.

Again,

If I were to cut out of a corn field one square acre, I add to 1 five cyphers, and then it is 100000; the root of which is 316 nearest, or 3 chains 16 links, and something more for the side of that acre.

To lay out any given quantity of acres in a right-angled parallelogram, whereof one side is given.

Turn first the acres into links, by adding as before five cyphers; that number thus increased divide by the given side, the quotient will be the other side.

Example.

It is required to lay out 100 acres in a parallelogram one side of which shall be 20 chains; first to the 100 acres I add five cyphers and it is 100,0000; which divide by 20 chains, or 2000 links; the quotient is 50 chains for the other side of the parallelogram.

(9)

Laying out land Continued. August 11<sup>th</sup> 1810.

To lay out any given number of acres in a parallelogram, one side of which shall be 4, 5, 6, or 7, &c. times longer than it is broad.

### Example.

Admit it were required of me to lay out 100 acres in a parallelogram, that should be 5 times as long as broad: first to the 100 acres I add 5 cyphers and it makes 100,0000; which sum I divide by 5 the quotient is 200000; the root of which is nearest 14 chains 14 links; and that I say, shall be the short side of such a parallelogram; and by multiplying that 14 14 by 5. shews me the longest side thereof to be 40 chains 40 links.

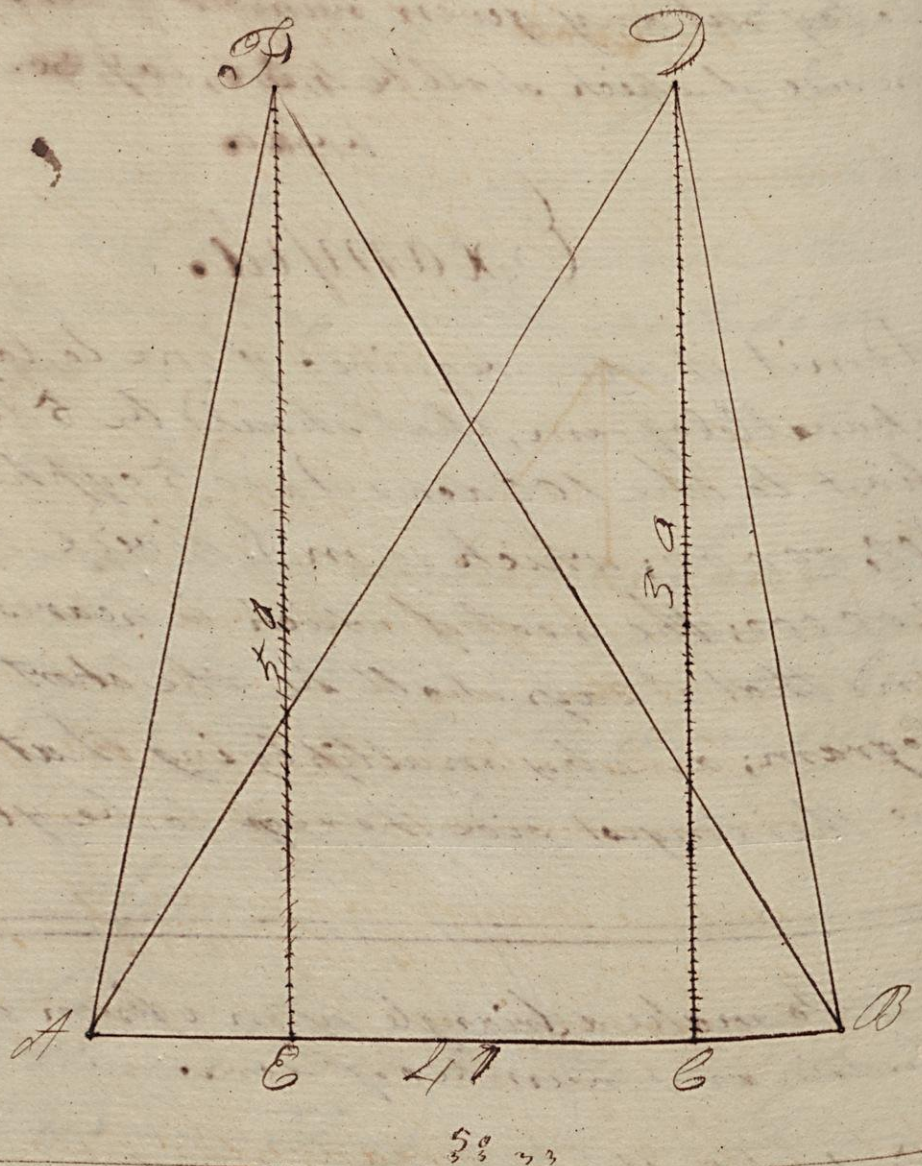
To make a triangle upon a given base, that shall contain any number of acres.

To double the given number of acres, annex 5 cyphers, and divide by the base, the quotient will be the length of the perpendicular required.

### Example.

Upon a given base whose length is 40 chains, I am to make a triangle that shall contain 100 acres, First, I double the 100 acres, and annexing 5 cyphers thereto it makes 200,0000; which I divide by 40 chains the given base; the quotient is 50 chains for the height of the perpendicular. As in this figure, AB is given base 40; on any part of it, as C, I make the perpendicular CD equal to 50 chains, and I draw the lines DC, CB, which make the triangle DCB, containing just 100 acres as required.

Laying out land Continued. August 11<sup>th</sup> 1810.



To find the length of the diameter of a circle which shall contain any number of acres required.

Say as 11 is to 14 so will the number of acres given be to the square of the diameter of a circle required.

Example.

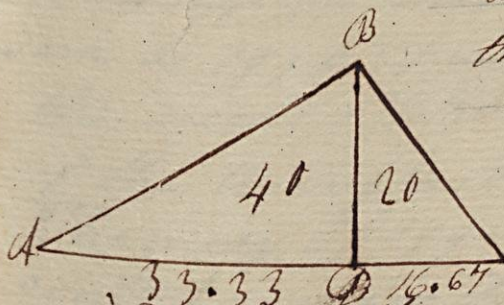
What is the length of the diameter of a circle, whose superficial content shall be 100 acres? Add 5 cyphers to the 100, and it makes 100,0000 links; which multiply by 14 facit 14000000, which divided by 11, gives for quotient 1272727 2 the root of which is 35 chains 67 links, and better almost 68 links, and so much shall be the diameter of the required circle.



(21)  
 Division of lands. August 13<sup>th</sup> 1840.

To divide a triangle several ways.

Suppose  $ABC$  a triangular piece of land containing 60 acres, to be divided between two men, one to have 40 acres cut off towards  $A$ , and the other 20 acres towards  $C$

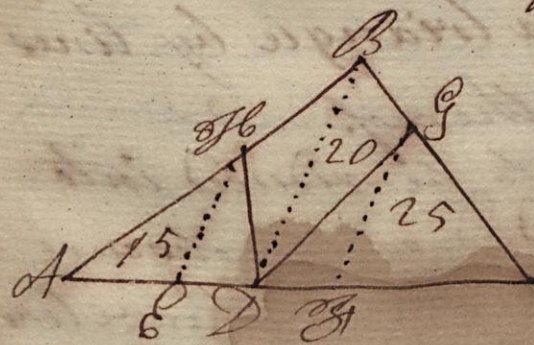


and the line of division to proceed from the angle  $B$ . First measure the base  $AC$ , viz. 50 chains; then say by the Rule of three, if the whole content 60 acres give 50 chains for its base

what shall 40 acres give? Multiply 40 by 50 and divide, the quotient will be 33 chains, 33 links; which set off upon the base from  $A$  to  $D$  and draw the line  $BD$ , which shall divide the triangle as was required

To divide a triangular piece of land into any number of unequal parts, by lines proceeding from any point assigned in any side thereof.

Let  $ABC$ , the triangular piece of land containing 60 acres, be divided between three men the first to have 15 acres the second 20 the third 25 acres and the lines of division to proceed from  $D$ ; first measure the base which is 50 chains; then divide the base into three parts as you have been before taught by saying if 60 give 50 what shall 15 give? Ans. 12 chains, 50 links for the



first man's base which set off from  $A$  to  $E$ . Again say, if 60 give 50 what shall 20 give? ans. 16 chains 66 links

for the second man's base; which set off from  $E$  to  $F$ ; then consequently the third man's base,  $FC$  viz. from  $F$  to  $C$ , must be 20 chains, 84 links. This done draw

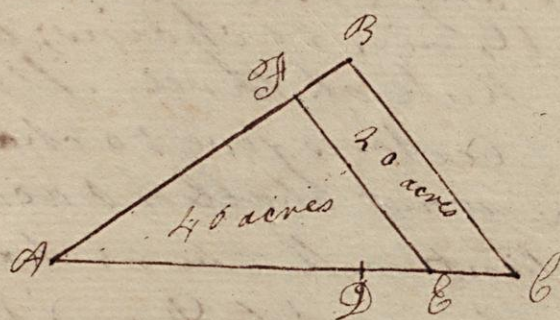
an obscure line from the point assigned  $D$ , to the opposite angle  $B$ ; and from  $E$  and  $F$  draw the lines  $ED$  and  $FD$  parallel to  $BD$ . Lastly from  $D$  draw the lines  $DE$  and  $DF$  which shall divide the triangle into three such parts as were required.

(22)

Division of Lands Continued August 14 1810.

To divide a triangular piece of land, according to any proportion given by a line parallel to one of the sides.

$ABC$  is a triangular piece of land containing 60 acres the base  $AC$  is 50 chains. This piece of land is



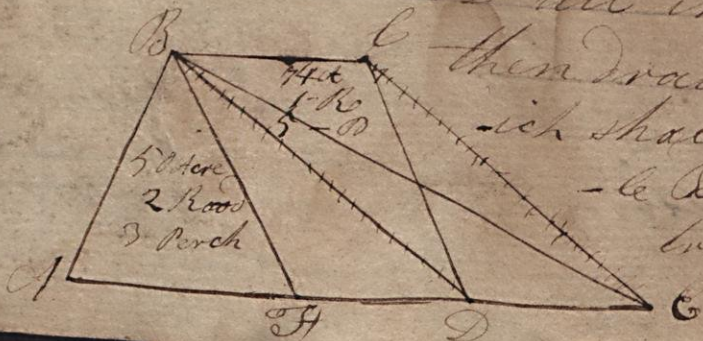
to be divided between two men by a line parallel to  $BC$  in such proportion that the one may have 40 acres and the other 20.

First divide the base as has been before taught and let the point of division fall in  $D$ ,  $AD$  being 33 chains, 33 links; and  $DC$  16 chains 67 links.

Secondly, Find a mean proportion between  $AD$  and  $AC$  by multiplying the whole base 50 by  $AD$  33, 33, the product is 1666.500; of which the square root being extracted, gives 40 chains, 62 links; set this off from  $A$  to  $E$ . Lastly, From  $E$  draw  $ED$  parallel to  $BC$ , which divides the triangle as Demanded.

To reduce a trapezium into a triangle by lines drawn from any angle thereof.

Let  $ABCD$  be the trapezium to be reduced into a triangle, and  $B$  the angle assigned. draw the obscure line  $BD$  and from  $C$  make a line parallel thereto as  $CE$  extend also the line  $AD$  till it meet  $CE$  in  $E$ .



then draw the line  $BE$ , which shall make the triangle  $BEC$  equal to the trapezium  $ABCD$ .

Continued. August 16 1810.

Division

Suppose the trapezium ABCD containing 124 acres, 3 roods, and 4 perches, is to be divided between two men the first to have 50 acres, 2 roods and 3 perches; the other 74 acres, 1 rood and 5 perches, and the line of division to proceed from B.

First, Reduce all the acres and roods into perches, then will the content of the trapezium be 19968 perches; the first man's share 8083 perches the second 11885.

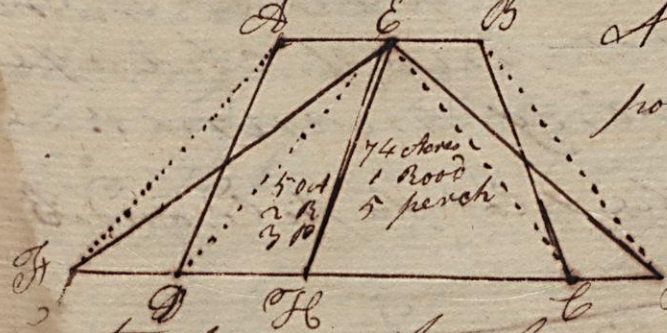
Secondly, Measure the base of the triangle, viz. A & 46 chains:

Then say, If 19968 the whole } 46 chains, 00 links, content give for its base

What shall 8083, the first } 31 chains, 52 links; man's part give? Answer

which set off from A to H, and drawing the line HB you divide the trapezium as desired; the triangle ABH being the first man's portion and the trapezium BCHA the second's.

How to reduce a trapezium into a triangle, by lines drawn from a point assigned in any side thereof



ABCD the trapezium, E the point assigned from whence to reduce it into a triangle

and run the division line. The trapezium is of the same content as the former, viz. 19968 perches; and it is to be divided as before, viz. one man to have 8083 perches, and the other 11885.

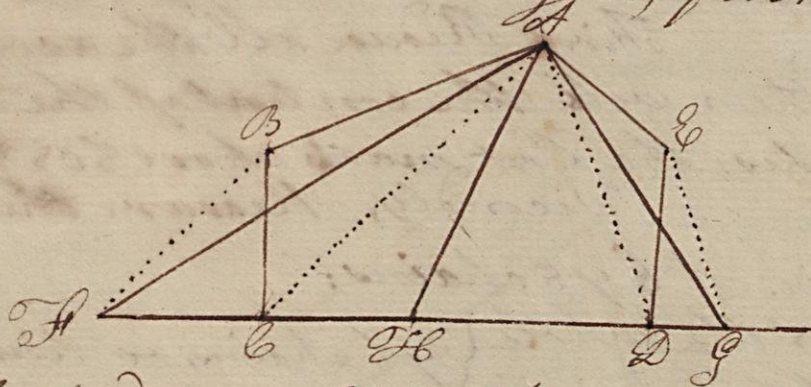
First, for to reduce it into a triangle, draw the lines EDC, and from A and B make lines parallel to them as AEG and BFG; then draw the lines EGF and the triangle EFG will be equal to the trapezium ABCD which is to be divided as before therefore find, by the rule of proportion, what the first man's base must be viz. 31 chains, 52 links, set it off from F to H, and draw the line HE, so shall you divide the trapezium according to the former proportion.

(24)

Division Land *Continued*. August 14<sup>th</sup> 1810. I 6

To reduce an irregular polygonal figure into a triangle and to divide the same into any given proportion

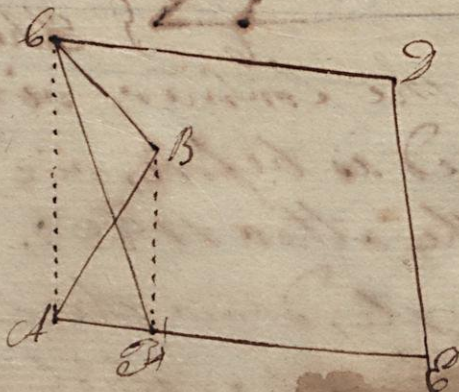
Let  $ABCDE$  be the five-sided figure; to reduce this into a triangle, first draw the lines  $AC$ ,



$AD$ ; and parallel thereto  $BF, EG$ , extending the base from  $C$  to  $F$ , and from  $D$  to  $G$ ; then draw the lines  $AF, AG$ , which will make the triangle  $AFG$  equal to the five-sided figure. If this were to be divided into two equal parts you must take  $HF$ , equal to half of the base of the triangle and from  $H$  draw the line  $HC$ , which divides the figure  $ABCDE$  into two equal parts.

If in dividing the plot of a field, there be outward angles, you may change them after the following manner.

Suppose  $ABCDE$  be the plot of a field, and  $B$  the outward angle.

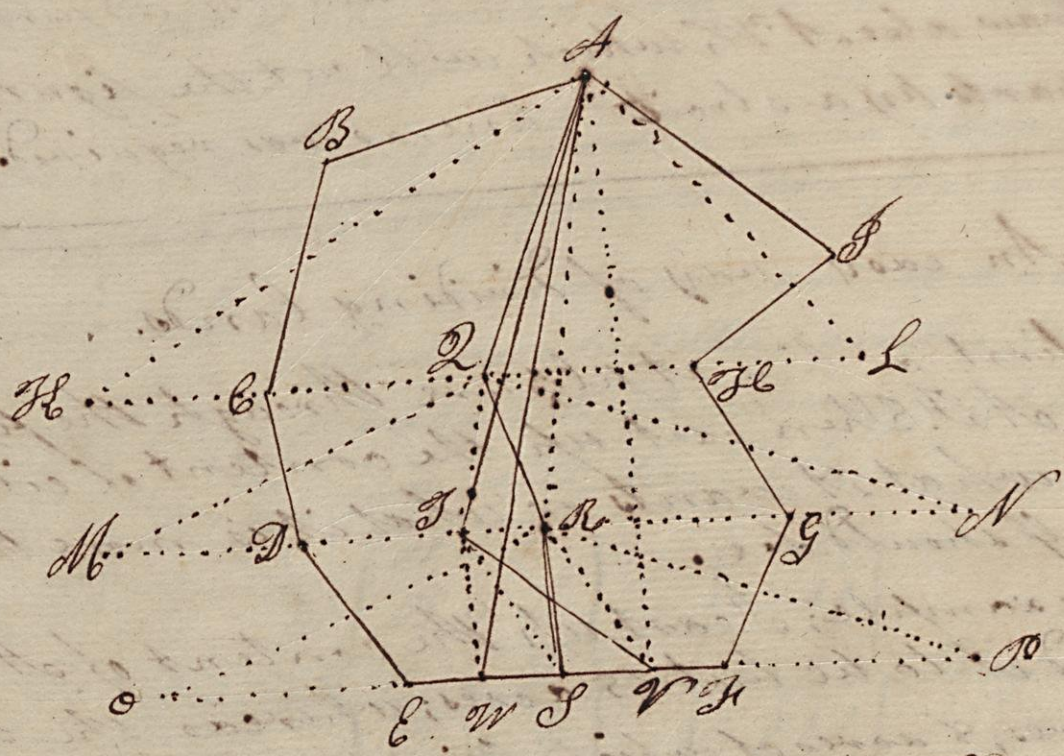


Draw the line  $CA$ , parallel thereto draw also  $BF$ ; join the points  $C, F$ , and the five-sided figure, having one angle, is now reduced into a four-sided figure or trapezium; which you may again reduce into a triangle, as has been before taught.

1810.

Continued. August 20

To divide an irregular plot of any number of sides according to any given proportion, by a straight line drawn through it.



$A B C D E F G H I A$  is a field to be divided equally between two men, by a straight line proceeding from  $A$ . First consider how to divide the field into five sided figures and trapezia, that you may the better reduce it into triangles, as by drawing the line  $B C$ , you cut off the five sided figure  $A B C D E$ , which reduce into the triangle  $A B C$ , and measuring half the base thereof, which will fall at  $Q$ , draw the line  $A Q$ .

Secondly, Draw the line  $M N$ , and from the point  $Q$  reduce the trapezium  $C D E F$  into the triangle  $M N Q$ ; which again divide into halves, and draw the line  $Q R$ .

Thirdly, From the point  $R$  reduce the trapezium  $D E F G$  into the triangle  $R D P$ , and taking half the base thereof draw the line  $R S$ , and then have you divided this irregular figure into two equal parts by the three lines  $A Q$ ,  $Q R$ ,  $R S$ .

Fourthly, Draw the line  $A R$ , also  $Q T$  parallel thereto, draw also  $A T$ , and then have you turned two of the lines into one.

(26)

Division Continued. August 22<sup>d</sup> 1810.

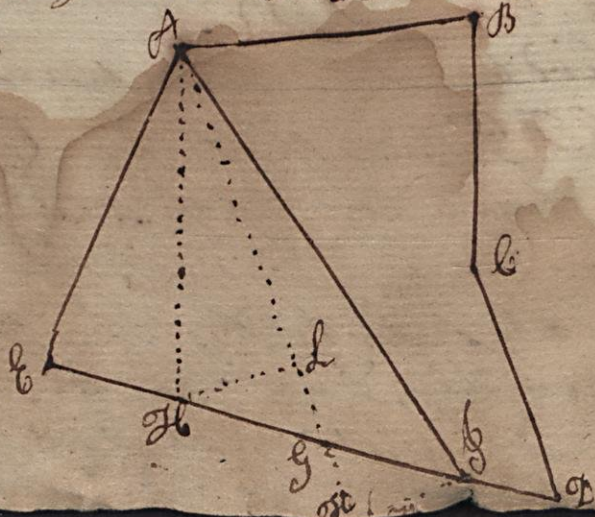
Fifthly, From *T* draw the lines *TS*, and parallel thereto the line *RT*. Draw also *TW*. Then is your figure divided into two equal parts by the two lines *TS* and *TW*. — Lastly, Draw the line *AV* and parallel thereto *TW*. Draw also *AV*, which will cut the figure into 2 equal parts by a straight line, as was required.

### An easy way of dividing lands.

Draw first a line at pleasure through the figure, as the line *AG*. Then cast up the content of either part and see what it wants or what it is more than the true half should be.

As for example; I cast up the content of *AGE*, and find it to be but 15 acres; whereas the true half is 23 acres; 8 acres of which being in the part *ABEDG* more than *AGE*. Therefore I make a triangle containing 8 acres, and add it to *AGE* as the triangle *AGI*; then the line *AI* parts the figure into two equal parts.

But more plainly to make this triangle: measure first the line *AG*, which is 23 chains 60 links. Double the 8 acres they make 16 to which add 5 cyphers to turn them into chains and links and then they make 160000; which divide by  $AG$  2360 the quotient is 6 chains 77 links; for the perpendicular *HI*, take from your scale 6 chains, 77 links, and set it so from the base *AGI*; that the end of the perpendicular may just touch the line *ED*, which suppose at *I*. Then draw the line *AI*, which makes the triangle *AGI* just 8 acres and divides the whole figure as desired.

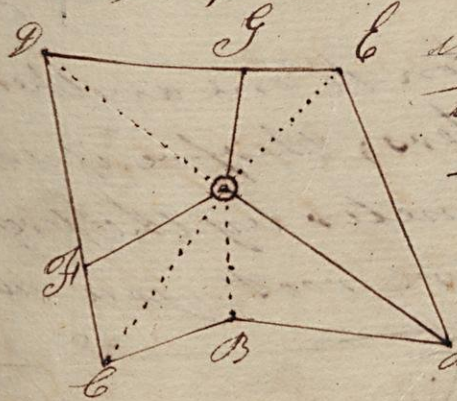


(27)

Division Continued August 23 1810.

Suppose a field containing 27 acres is to be divided between 3 men each to have 9 acres and the lines of division to run from a pond in the field so that each person may have the benefit of the water, without going over another's land.

First from the pond draw lines to every angle as  $oA, oB, oC, oD, oE$ ; and then is the figure divided into 5 triangles; measure each of these and put their contents down separately which reduce into perches and you will have the



|          |         |    |      |          |
|----------|---------|----|------|----------|
| Triangle | }       | be | }    | Perches. |
|          | o A o B |    | 674  |          |
|          | o B o C |    | 390  |          |
|          | o C o D |    | 1238 |          |
|          | o D o E |    | 911  |          |
|          | o E o A |    | 1107 |          |

The whole content is 4320 perches or 27 acres, and each man's proportional part 1440 perches. From  $o$  to any angle draw a line for the first division-line, as  $oA$ , then consider that the first triangle  $oAB$  is but 674 perches, and the second  $oBC$  390 both together but 1064 perches less by 376 than 1440 one man's portion. You must therefore cut off from the third triangle  $oCD$  376 perches for the first man's dividing line, which you may do thus: the Base  $oC$  is 18 chains the content of the triangle 1238 perches; say then, if 1238 perches give the base 18 chains, what shall 376 perches give? Ans. 5 chains, 45 links; which set off from  $oC$  to  $F$ , and drawing the line  $oF$  you have the first man's part, viz.  $oFA$  &  $oAB$ . Secondly, Observe the remaining part of the triangle  $oBC$  after 376 is taken out and you will find it to be 14 perches, which is less than 1440 by 578. Therefore from the triangle  $oDE$  cut off 578

Division. <sup>(P. 8)</sup> Continued. August 23 1810

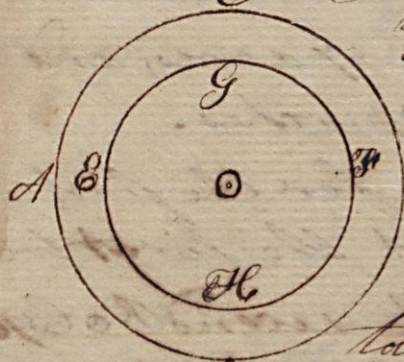
perches and in the point of division will fall in G.  
Draw the line OG, which with OG and O B, divides the  
figure into 3 equal parts.

To divide a circle according to any proportion by  
a line concentric with the first.

The areas of circles are in proportion to one another  
as the squares of their semidiameters; therefore, if you  
divide the square of the semidiameter by the propor-  
tion given, and extract the square root you will  
have your desire.

### Example.

ABCD be a circle to be equally divided between two  
men. 9/35



The diameter thereof is 2 chains.

The semidiameter 1 chain or 100 links.

The square thereof 10000.

Half the square 5000.

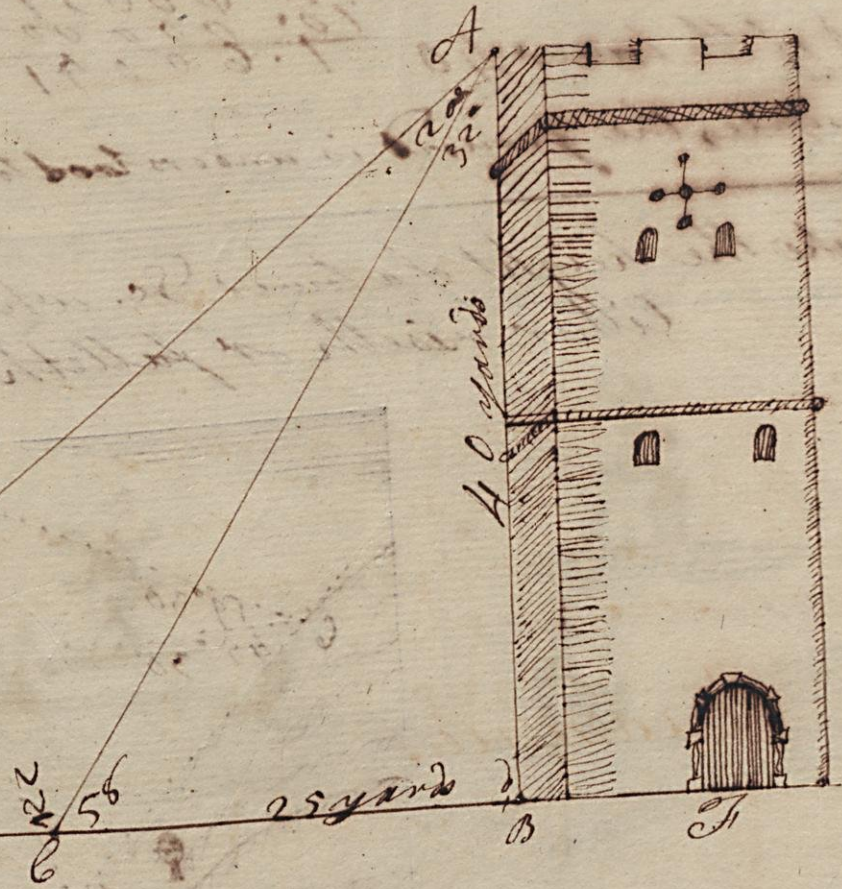
The root of the half 71 links, which  
take from your scale, and upon the same  
center describe the circle GEH, which  
will divide the circle into two equal parts.

ABCD



# Of Heights and Distances.

To take the height of a tower, steeple, tree, or any such thing.



As the angle sine at  $32^\circ$   $9.724210$   
 So to the Base  $25$   $1.397940$   
 So is the sine angle  $65^\circ$   $9.928420$   
 To the height of tower  $A. B. 40$   $7.602150$

To take the height of a tower &c. when you cannot come near the foot thereof.

In the fore going figure, let  $A. B.$  represent the tower; and  $C. B.$  meat, or some other hindrance that you cannot come nigher than  $C.$  to take the height. Therefore at  $C.$  place your instrument right so that you may take the angle  $A. C. B. 58^\circ$ . Then go backward any convenient distance as to  $G.$  there also take the angle  $A. G. B. 38^\circ$ . This done subtract  $58$  from  $180$ , to have you  $122$  deg. the angle  $A. G. C.$  Then  $122$  and  $38$  being taken from  $180$  remain  $20$  for the angle  $G. A. C.$  the Dist.  $G. C. 20$  yards.

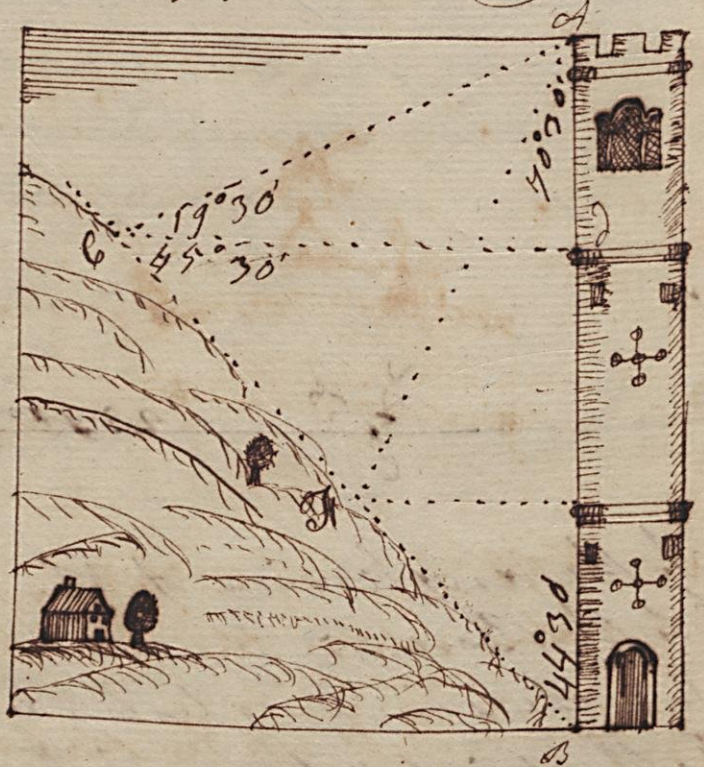
As sine angle at  $20$   $9.534052$   
 So to  $G. C. 20$   $11.414993$   
 So is the sine angle  $G. 38$   $9.789342$   
 To the line  $A. C. 47$   $11.204318$   
 $1.670263$

Heights Continued. August 24<sup>th</sup> 1810

|                               |           |
|-------------------------------|-----------|
| As Radius 100                 | 10.000000 |
| Is to the line AC 49          | 1.467209  |
| So is the sine angle C 58     | 9.928420  |
|                               | <hr/>     |
|                               | 1.600518  |
|                               | 10.000000 |
|                               | <hr/>     |
| To the height of the tower 40 | 1.600518  |

In this example, the ground is understood to be level.

How to take the height of a tower &c. when the ground either riseth or falleth.

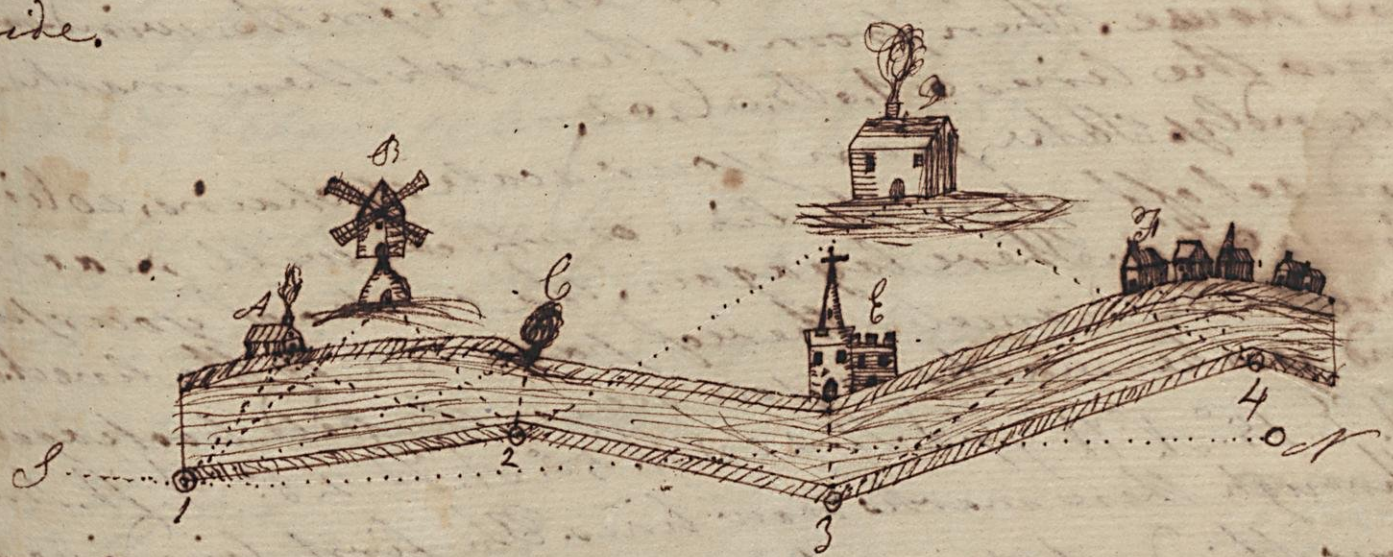


|                                       |           |
|---------------------------------------|-----------|
| As the sine of angle C 49° 30'        | 9.944346  |
| Is to the dist. CB 36 yards           | 1.448188  |
| So is the <sup>sine</sup> angle C 58° | 9.957296  |
|                                       | <hr/>     |
|                                       | 11.705464 |
|                                       | 9.944346  |
|                                       | <hr/>     |
| To the height of tower 54 yards       | 1.731178  |

To take this at 2 stations without approaching the foot of the tower you must proceed as before directed for if you take the angles at C and then measure to F and there, in like manner as before take your angle again there by you may find all the angles and the line CF then say, as the sine of the angle CFB Is to the log. of the line FA So is the sine of the angle AFB So the log. of of the height of the tower AB

(31)  
 Of Distance. August 27<sup>th</sup> 1810.

Having before shewed you how take the proper distances in surveying a field at two stations yet as it naturally occurs in this place I will give you one example the river, suppose the following figure to be part of a river, and you being measuring along on one side of it, all desirous to know the breadth of it as also to make a true plot thereof, by putting down what remarkable things are seen on the other side.



Observation 1  
 N. W. 6° and 15 chains, 20 links, equal to 02.  
 A tree upon the brink of the river bears  
 N. W. 19° 00'.  
 A windmill up in the land  
 N. W. 40° 00'.  
 A house upon the river bank  
 N. W. 52° 00'.

02 N. E. 15° and 18 chains, 20 links, equal to 03  
 The tree N. W. 44°  
 The house S. W. 20°  
 The wind-mill S. W. 50° } these look back to the observation of 01.  
 A noted house far up in the land N. W. 28° } Forward observations.  
 A church upon the rivers bank N. W. 60° }

03 N. W. 15° and 20 chains, 50 links equal to 04.  
 The church bears N. W. 88° } These look back to the obs. of 02  
 The noted H. cannot be seen } at forward observation  
 The end of a little village N. W. 32° }

(32)

Distance Continued. August 28<sup>th</sup> / 1810. Q

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④  
The end of the little village }  
  S.W. 32° } These respect ③  
The house respecting ② in } and ②.  
the land                       S.W. 34° }

---

To protract this draw the line  $A.B.$  for a meridian and laying the protractor upon it the center thereof to ①; against  $N.W. 6^{\circ}$  make a mark for the line that goes to ②; also against  $N.W. 17^{\circ}$  make a mark for the tree and against  $40^{\circ}$  and  $52^{\circ}$  for the wind-mill and house. Then from ① through these marks draw the lines  $A.C.$ ,  $A.B.$ , and  $C.②$ .

Secondly, Take from your scale 18 chains, 20 in. and set off upon the line  $A.B.$  which will reach from ① to ②. There lay again the center of your protractor the diameter thereof parallel to the line  $A.B.$ ; and make marks as you see in the field-book against  $N.E. 15^{\circ}$ ,  $N.W. 44^{\circ}$ ,  $S.W. 20^{\circ}$ ,  $S.W. 50^{\circ}$ ,  $N.W. 28^{\circ}$ ,  $N.W. 4^{\circ}$  and through these marks draw lines. The first line directs to your third station, the second line  $N.W. 40^{\circ}$  directs you to the tree  $C$  upon the rivers bank; for that line cutting the line  $A.C.$ , shews you by the intersection where the tree stood and also the breadth of the river. Also the line  $S.W. 20^{\circ}$  cuts the line from the first station  $N.W. 52^{\circ}$  in the place where the house  $D$  stands upon the bank of the river. If therefore you draw a line from  $A$  to  $C$ , it will represent the farther bank of the river. ~~If therefore you draw a line from  $A$  to  $D$~~  so you may proceed on plotting, according to the notes in your field-book; and you will not only have a true plot of the river but also know how far the wind-mill  $B$ , and the house  $D$ , &c. stand from the water-side. ○

# How to take the horizontal line of a hill

Suppose A B C a hill whose base you would know.  
 Place your semicircle at A and cause a mark to be  
 set up at B, as high above the top of the hill as  
 instrument stands from the ground at A; and with  
 your instrument horizontal take the angle B  
 A C 58 deg. Measure the dist. A B. 1600 & 8 links;

then say,  
 As Radius, 10.000000  
 So to the line A B, 60.800. 3.225309  
 So is the sine comp. of 58° 9.724210  
 To 12.949519  
 To get A D 8 chains, 90 links, 2.949519

But if you have occasion to measure the whole hill,  
 place again your instrument at B and take the angle  
 C B D, which suppose 46 deg. Measure also the Dist.

B C 21 chains; then say,  
 As Radius 10.000000  
 So to the line B C 21 ch. 1.322219  
 So is the sine of the angle C B D 46 9.856984  
 To 11.179153  
 To the remaining part of the base D C 150.112. 1.179153

Which added to 8.90 makes 24 chains & 1 link, for the  
 whole base A C; which is to be plotted, instead of A B or  
 B C; although they were used in finding the content  
 of the land.

I mentioned this way for your better understanding  
 how to take the base of part of a hill; for it often  
 happens your survey ends upon the side of a hill.

But if you find you are to take in the whole hill  
 you may facilitate the work by the former way.

Thus: take, as before the angle at A 58 deg. Measure also  
 A B. Then at B take the whole angle C A B 48°.  
 Subtract the sum of these angles from 180 deg. remain  
 44 for the angle at C; then say,  
 As the sine of the angle C  
 So to the side A B  
 So is the sine of the angle A B C  
 To the log. of the base A C. August 31<sup>st</sup> 1810

How to take the ...

... to be ...

|          |
|----------|
| 10.00000 |
| 3.02789  |
| 9.97211  |
| 2.97211  |
| 2.97211  |
| 2.97211  |

... to be ...

|         |
|---------|
| 1.12222 |
| 1.82222 |
| 1.17777 |
| 1.17777 |

... to be ...

... to be ...

... to be ...

... to be ...

(35) Sept. 5<sup>th</sup> 1812.

# Miscellaneous Questions.

In an Orchard of fruit trees  $\frac{1}{2}$  of them bear apples  $\frac{1}{4}$  Pears,  $\frac{1}{6}$  Plums 60 of them Peaches and 40 cherries How many trees does the Orchard contain?

$\frac{1}{2} + \frac{1}{4} + \frac{1}{6} = \frac{12}{12} + \frac{3}{12} + \frac{2}{12} = \frac{17}{12}$  and  $\frac{17}{12} - \frac{12}{12} = \frac{5}{12}$  therefore, As  $\frac{5}{12} : \frac{60+40}{1} :: \frac{12}{5} : 1200$  Ans.

A person who was possessed of  $\frac{2}{5}$  of a vessel, sold  $\frac{5}{8}$  of his interest for £375; what was the ship worth at that rate?  $\frac{5}{8}$  of  $\frac{2}{5} = \frac{1}{4}$ . As  $\frac{1}{4} : 375 :: \frac{4}{1} : £1500$  Ans.

If  $\frac{5}{7}$  of  $\frac{3}{8}$  of  $\frac{4}{5}$  of a ship be worth  $\frac{2}{7}$  of  $\frac{4}{8}$  of  $\frac{12}{13}$  of the cargo valued at 1000 £: what is both ship and cargo cost?

$\frac{5}{7}$  of  $\frac{3}{8}$  of  $\frac{4}{5} = \frac{28}{35}$ , and  $\frac{2}{7}$  of  $\frac{4}{8}$  of  $\frac{12}{13}$  of  $\frac{1000}{1} = \frac{4000}{39}$ , then  
As  $\frac{28}{35} : 4000 :: \frac{35}{28} : \frac{28 \times 4000 \times 28}{28} = £837, 12, 01 \frac{25}{39}$  the cost of the ship and £1000 + £837, 12, 01  $\frac{25}{39}$  = 1837 £ 12, 01  $\frac{25}{39}$  Value of the Ship and cargo, etc.

Two ships A and B sailed from a certain port at the same time; A sailed north 8 miles an hour, and B East 6 miles an hour Required, by an easy method, their Distance asunder at every hours end?

$\sqrt{8 \times 8 + 6 \times 6} = 10$  miles distant in 1 hour, and  $10 \times 2 = 20$  miles in 2 hours, &c. Answer.

If a body be weighed in each scale of a balance, whose Beam is unequally divided, and those different weights of the body be multiplied together the square root of the Product will be the true weight of the body. Suppose the weight of a bar of silver in one scale be 10 oz. and in the other scale 12 oz. Required the true weight of the bar?

oz.                      oz.    part.    gr.  
 $\sqrt{12 \times 10} = 10, 954 = 10 \text{ } 19 \text{ } 1, 92$  Ans.

N. 2. Continued. September 6<sup>th</sup> 1810. Q

A younger brother received 1560 £, which was just  $\frac{2}{3}$  of his elder brother's fortune; and  $3\frac{1}{2}$  times the elder's money was  $\frac{2}{3}$  as much again as the Father was worth; Pray what was his estate valued at?

As 7 : 1560 :: 12 : 2674  $\frac{2}{3}$  the elder brother's fortune, then  
 $2674\frac{2}{3} \times 5\frac{1}{2} = \frac{2}{3} = \text{£ } 19165\ 14\text{s } 3\frac{1}{4}\text{d}$  Ans.

A Gentleman divided his fortune among his sons giving to A 9 as to B 5, and to C but 3 £ as often as to B; and yet C's dividend was £ 1537  $\frac{5}{8}$ ; what did the whole Estate amount to?

As 7 : 5 :: 3 : 2  $\frac{1}{2}$  then As 2  $\frac{1}{2}$  : 1537  $\frac{5}{8}$  :: 9 + 5 + 2  $\frac{1}{2}$  : £ 11583  
8s 1d Ans.

A Gentleman left his son a fortune;  $\frac{5}{16}$  of which he spent in 3 months;  $\frac{3}{4}$  of  $\frac{5}{16}$  of the remainder lasted him 9 months longer when he had only £ 537 left; Pray what did his Father bequeath him?

$\frac{1}{16}$  = whole legacy,  $\frac{1}{16} - \frac{5}{16} = \frac{1}{16}$  left at 3 months, then  $\frac{3}{4}$  of  $\frac{1}{16}$  of  $\frac{1}{16}$   
 $= \frac{165}{384}$  and  $\frac{1}{16} = \frac{165}{384} = \frac{1584}{6144} = \text{£ } 537$ , therefore, as  $\frac{1584}{6144} : 537 :: 1$   
: £ 2082 18s 2  $\frac{3}{4}$  Ans.

A gay young fellow soon got the better of  $\frac{2}{3}$  of his fortune; he then gave £ 1500 for a commission and his profusion continued till he had but 450 £ left which he found to be just  $\frac{1}{6}$  of his money after he had purchased his Commission; what was his fortune at first?

As 6 : 450 :: 16 : 1200, and  $1200 + 1500 = \text{£ } 2700 = \frac{2}{3}$  of his fortune, and as 5 : 2700 :: 7 : £ 3780 Ans.



Q2. Continued. Sept. 13<sup>th</sup> 1810.

A has £100 of B's money in his hands for the service of which B allows him 9 per cent. What sum must he remit to discharge himself of the 100 £?

As 100 + 9 : 100 :: 100 : £ 91 <sup>81</sup>/<sub>109</sub> or  $\frac{100 \times 100}{100 + 9} = 91 \frac{81}{109}$  to be remitted, and  $\frac{100 \times 9}{100 + 9} = £ \frac{26}{109}$  his Commission.

If 15 men can perform a piece of work in 10 days; How many men will accomplish another piece of work 4 times as large in  $\frac{1}{5}$  of that time?

Work. Men. Works. Men. Time. Men. Time. Men. Time. Men.  
 As 1. : 15 : : 4 : 60 : :  $\frac{1}{5}$  : 300 : : Ans.

If A can do a piece of work in 9 days and B in 12; set them both about it together; in what time will they finish it?

Work. Work. Work. Work. Day. Work. Day. Work. Day.  
 As } 9 : 1 : : 1 :  $\frac{1}{9}$  } They  $\frac{1}{9} + \frac{1}{12} = \frac{7}{36}$  : :  $\frac{36}{7}$  : : 5  $\frac{1}{7}$  : : Ans.

A and B together can build a Boat in 20 days; with the assistance of C they can do it in 12; In what time would C do it by himself?

D. W. D. W. D. W. D. W. D. W.  
 20 : 1 : : 1 :  $\frac{1}{20}$  } 12 : 1 : : 1 :  $\frac{1}{12}$  }  $\frac{1}{20} + \frac{1}{12} = \frac{7}{60}$  : :  $\frac{60}{7}$  : : 8  $\frac{4}{7}$  : : Ans.

A can do a piece of work alone in 13 days, and A and B together in 8 days; In what time can B do it alone?

D. W. D. W. D. W. D. W.  
 13 : 1 : : 1 :  $\frac{1}{13}$  } 8 : 1 : : 1 :  $\frac{1}{8}$  }  $\frac{1}{13} + \frac{1}{8} = \frac{21}{104}$  : :  $\frac{104}{21}$  : : 4  $\frac{8}{7}$  : : Ans.

(38)

M. 2. Continued. Sept. 13<sup>th</sup> 1810.

A cistern for water has 2 cocks to supply it by the first it may be filled in 45 minutes and by the second in 53 minutes; it has likewise a discharging cock by which it may when full be emptied in 30 minutes; now if these cocks be all left open when the water comes in in what time will the cistern be filled?

|   |  |  |
|---|--|--|
| Min. Cist. Min.<br>45 : 1 : 60<br>$\frac{45}{150} = \frac{1}{3}$<br>$\frac{150}{150} = 1$<br>$\frac{135}{150} = \frac{9}{10}$<br>$\frac{135}{150} = \frac{9}{10}$<br>$\frac{135}{150} = \frac{9}{10}$<br>$\frac{135}{150} = \frac{9}{10}$ | Min. Cist. Min.<br>55 : 1 : 60<br>$\frac{55}{330} = \frac{1}{6}$<br>$\frac{330}{330} = 1$<br>$\frac{275}{330} = \frac{5}{6}$<br>$\frac{275}{330} = \frac{5}{6}$<br>$\frac{275}{330} = \frac{5}{6}$ | Cist. Hour. Cist. Min.<br>4242 : 1 : 1<br>$\frac{4242}{4242} = 1$<br>$\frac{4242}{4242} = 1$<br>$\frac{4242}{4242} = 1$<br>$\frac{4242}{4242} = 1$ |
|---|--|--|

H. M. S.  $2 \frac{1}{2}$  Ans.

$\frac{90960}{4242} = 21 \frac{1}{2}$   
 $\frac{6120}{4242} = 1 \frac{1}{2}$   
 $\frac{4242}{4242} = 1$   
 $\frac{4242}{4242} = 1$   
 $\frac{4242}{4242} = 1$

A Water-tub holds 73 Gallons; the pipe which conveys the water to it usually admits 4 Gals. in 5 Min.; and the Tap discharges 20 Gals. in 14 Min.; now supposing these both to be carelessly left open, and the water to be turned on at 4 o'clock in the morning; a Servant at 6 finding the water running puts in the Tap; In what time after this accident will the Tub be full?

Min. Gal. Min. Gal.  $84 - 40 \frac{10}{17} \times 2 = 29 \frac{14}{17}$  gal. &  $73 - 26 \frac{14}{17} =$   
 $46 \frac{17}{17}$  gal. which now remains to be filled  
 Therefore, at 4 : 5 : 46  $\frac{17}{17}$  : 32  $\frac{14}{17}$  and therefore the Tub will  
 be full at 32  $\frac{14}{17}$  after 6.

The hour and minute hand of a watch are exactly together at 12 o'clock; when are they next together? The velocities of the two hands of a watch, or clock are to each other, as 12 to 1; therefore, the difference of velocities is 12 - 1 = 11.

|  |  |  |
|--|--|--|
| $\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$ | $\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$ | $\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$<br>$\frac{11}{11} = 1$ |
|--|--|--|

Continued. Sept. 17<sup>th</sup> 1810.

No. 2.

A hare starts 12 rods before a hound; but is not perceived by him till she has been up 45 seconds; she scuds away at the rate of 18 miles an hour, and the dog, on view, makes after, at the rate of 16 miles an hour; How long will the course hold; and what space will he run over, from the spot where the dog started?

$\frac{16}{18} = \frac{8}{9}$  or as 8 to 9 against the hare. 1 hour = 3600 sec.  
3600 : 52800 :: 115  
204060  
271200  
36000  
246000  
246000

2288 run over by the dog.

94 1/2 seconds.

12 rods = 660 feet  
36864 feet  
288 feet  
84480 : 3600 :: 2288  
1392500  
6864  
84480  
2336800  
760320  
638600  
597360  
42340  
84480

A Fellow said that when he counted his nuts 2 by 2, 3 by 3, 4 by 4, 5 by 5, 6 by 6, there was a tally an odd one; but when he told 7 by 7 they came out even; How many had he?

3  
6  
14  
120  
720  
7721 Ans.  
103 even.

2, 3, 4, 5, 6, respectively will leave an odd one.

M. Questions Continued Sept. 18<sup>th</sup> 18<sup>o</sup>.

There is an Island, 50 Miles in circumference and 3 men start together to travel the same way about it: A goes 4 miles per day B 6 and C 9; when will they come together again, and how far will each travel?

|     |     |      |    |
|-----|-----|------|----|
| 59  | 58  | 59   | 9  |
| 350 | 400 | 450  | 4  |
|     |     | 350  | 24 |
|     |     | 1200 |    |

24 1/2 days A 350 Miles B 400 and C 450 Miles

Suppose A leaves Newburyport at 6 o'clock on Monday morning, and travels towards Providence at the rate of 4 miles per hour without intermission, and that at 3 in the afternoon B sets out from Providence for Newburyport and travels constantly at the rate of 5 1/2 miles per hour; Now suppose the distance between the two towns to be 90 miles; where about on the road will they meet?

3 hours the time A had travelled before B started

36 miles the Distance

1 1/4 miles per hour

36 miles remain to be travelled by both

1 1/4 of 34 + 36 = 55 1/4

54 / 17 1/2 = 3 1/2

36 1/2 / 5 1/2 = 7

7 - Newburyport which is near as far as Dedham

If during Ebb-tide a wherry should set out from Haverhill to come down the river, and at the same time another should set out from Newburyport to go up the river allowing the distance to be 18 miles. Suppose the current forwards one and retards the other 1 mile per hour; the boats are equally laden the rowers are equally good and in common way of working in still water, would proceed at the rate of 4 miles per hour; where in the river will the two boats meet?

# Continued. Sept. 19<sup>th</sup> 1810.

M. Questions

$$\frac{1 \frac{1}{2}}{5 \frac{1}{2}} + 1 \frac{1}{2} = 5 \frac{1}{2} \text{ and } \frac{1 \frac{1}{2}}{2 \frac{1}{2}} = 2 \frac{1}{2} \text{ then } \frac{5 \frac{1}{2} + 2 \frac{1}{2}}{8} = 8 \text{ in 1 hour by leath}$$

$$\frac{10}{8} : 1 :: \frac{10}{9} = 2 \frac{1}{4} \text{ then } 5 \frac{1}{2} \times 2 \frac{1}{4} = 12 \frac{3}{8} \text{ from Flaverhill}$$

$$\text{and } \frac{2 \frac{1}{2}}{4} \times 2 \frac{1}{4} = 5 \frac{5}{8} \text{ from Newburyport}$$

Three Persons purchase a vessel in company, towards the payment of which A advanced  $\frac{2}{5}$  B  $\frac{3}{5}$  and C  $\frac{1}{5}$  £; what part and how much each pay and what part of the vessel had C?

$$\frac{2}{5} + \frac{3}{5} = \frac{14+15}{35} = \frac{29}{35} \text{ and } \frac{35}{35} - \frac{29}{35} = \frac{6}{35} \text{ C's part of the vessel}$$

$$\frac{14}{35} : \text{£ } 97 \frac{8}{8} \text{ advanced.}$$

$$\frac{15}{35} : \text{£ } 40 \text{ B advanced.}$$

$$\frac{6}{35} : \frac{256}{1} :: \frac{14}{35} : \frac{256}{1} :: \frac{15}{35} : \frac{256}{1} :: \frac{6}{35} : \frac{256}{1}$$

$$\frac{35}{6} \cdot \frac{256}{1} = \frac{14}{35} \cdot \frac{256}{1} = \frac{15}{35} \cdot \frac{256}{1} = \frac{6}{35} \cdot \frac{256}{1}$$

$$210 \overline{) 12544} \text{ 40 } \text{£ } 597 \frac{8}{8}$$

$$210 \overline{) 12544} \text{ 40 } \text{£ } 640$$

M. Questions Continued. Sept. 21<sup>st</sup> 1810.

A, B, and C are to share 100£ in the Proportion of  $\frac{1}{3}$   $\frac{1}{4}$  and  $\frac{1}{5}$  respectively; but C dying it is required to divide the whole sum properly between the other two?

As  $\frac{1}{3} + \frac{1}{4} + \frac{1}{5} : 100 :: \left\{ \begin{array}{l} \frac{1}{3} : 42 \frac{26}{75} \text{ A's} \\ \frac{1}{4} : 31 \frac{23}{75} \text{ B's} \\ \frac{1}{5} : 25 \frac{25}{75} \text{ C's} \end{array} \right\}$        $\frac{1}{3} + \frac{1}{4} + \frac{1}{5} = \frac{4+5+9}{20} = \frac{18}{20}$

$\frac{60}{47} : 100 :: \frac{1}{3}$

$\frac{60}{47} : 100 :: \frac{1}{4}$

$\frac{60}{47} : 100 :: \frac{1}{5}$

$$\begin{array}{r} 6000 \\ 141 \overline{) 6000} \quad 42 \\ \underline{564} \\ 360 \\ 3141 \overline{) 360} \\ \underline{282} \\ 78 \\ 49 \overline{) 78} \\ \underline{49} \\ 29 \end{array}$$

$$\begin{array}{r} 10000 \\ 788 \overline{) 10000} \quad 31 \\ \underline{564} \\ 4188 \\ 47 \overline{) 4188} \\ \underline{4142} \\ 46 \end{array}$$

$$\begin{array}{r} 6000 \\ 233 \overline{) 6000} \quad 25 \\ \underline{4800} \\ 1200 \\ 5235 \overline{) 1200} \\ \underline{1125} \\ 75 \\ 47 \overline{) 75} \\ \underline{47} \\ 28 \end{array}$$

$$\begin{array}{r} 264 \\ 47 \overline{) 264} \\ \underline{238} \\ 26 \\ 47 \overline{) 26} \\ \underline{21} \\ 5 \end{array}$$

$$\begin{array}{r} 42 \\ 56 \\ 12 \\ 10 \\ 14 \\ 5 + \frac{1}{4} = \frac{7}{2} \end{array}$$

As  $\frac{1}{3} + \frac{1}{4} : 25 \frac{25}{47} :: \frac{1}{5} \frac{14}{47}$

$$\begin{array}{r} 25 \\ 19 \frac{1}{2} \\ 10 \frac{1}{2} \\ 11 \frac{1}{2} \\ 1200 \\ 47 \end{array}$$

$$\begin{array}{r} 12 : 1200 :: \frac{1}{3} 1200 \\ 7 : 42 \\ 329 \\ 987 \end{array}$$

$$\begin{array}{r} 582 \\ 47 \overline{) 582} \\ \underline{428} \\ 154 \\ 2328 \\ 29354 \\ 25662 \\ 27354 \\ 27016 \\ 46389 \end{array}$$

$$\begin{array}{r} 46389 \overline{) 53016} \\ \underline{46389} \\ 6627 \\ 46389 \overline{) 32540} \\ \underline{29274} \\ 3276 \\ 46389 \overline{) 297144} \\ \underline{46389} \\ 13254 \\ 46389 \overline{) 53016} \\ \underline{46389} \\ 6627 \end{array}$$

$$\begin{array}{r} 100.0.0.0 \\ 57.2.10.14 \\ \hline 42.17.01.34 \end{array}$$

S. D. Div.  
 £. 57 - 2 - 10 - 14 A's share  
 S. D. Div.  
 £. 42 - 17 - 1 - 34 B's share

John Dorring, Easthampton

2. Continued. Sept. 22<sup>d</sup> 1810.

Miscellaneous  
There are 3 horses, belonging to different men employed as a team to draw a load of salt from Newburyport to Boston for £100. A and B are supposed to do 3/7 of the work; A and C 1/4 and B and C 1/4 of it; they are to be paid proportionably; can you divide it as it should be?

$$\begin{array}{l}
A + B = \frac{3}{7} = 2727 \\
A + C = \frac{1}{4} = 3846 \\
B + C = \frac{1}{4} = 2857 \\
\hline
\text{Sum } 9430
\end{array}$$

And  $943 \div 2$ , the number combined

$$\begin{array}{r}
9430 \\
4715 \\
\hline
= 4715 = A + B + C \\
- 2727 = A + B \\
\hline
= 1988 = C
\end{array}$$

Then, as,  $4715 : 30 :: 198 \frac{2}{3} : \text{£} 110 \frac{3}{4}$

$$\begin{array}{r}
4715 \overline{) 99400} \text{ (happy)} \\
\underline{5190} \\
4115 \\
\underline{3855} \\
4620 \\
\underline{4150} \\
460 \\
\underline{4355}
\end{array}$$

$1.10 \frac{3}{4} = C$

In the same manner proceed for the rest

Being about to plant 5292 fruit trees in rows the length of the grove is to be 3 times the breadth; how many of the shorter rows will there be?

$\sqrt[3]{5292} \times 3 = 126$  rows. Ans.  $\frac{1}{3}$  of the trees are to form an exact square the side whereof being 42, shows how many come into a short row.

$$\begin{array}{r}
3 \overline{) 5292} \\
\underline{1176} \\
3516 \\
\underline{3516} \\
0
\end{array}$$

Decorative flourish at the bottom of the page.

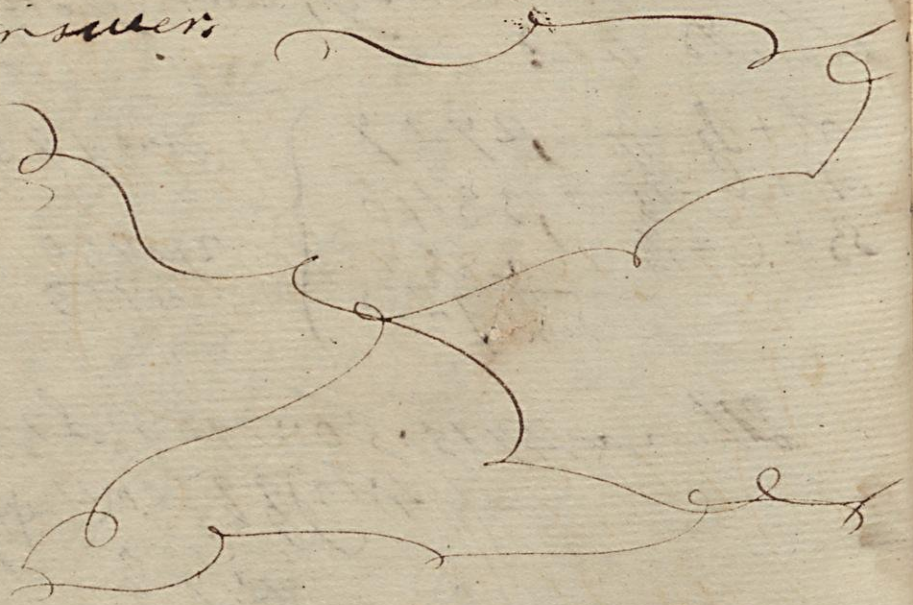
(44)

Mr. Questions

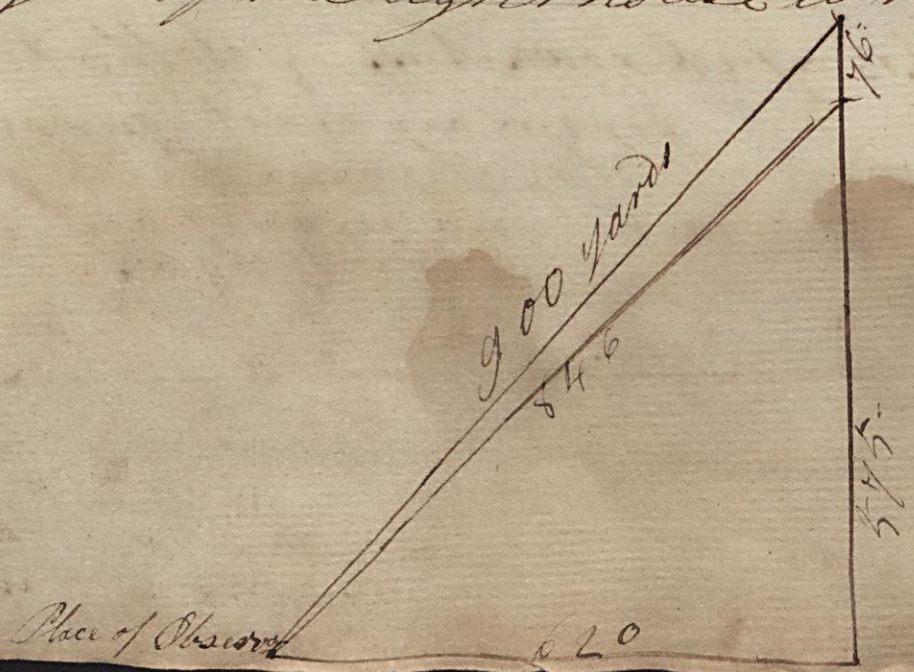
Continued October 4<sup>th</sup> 1800

A General, disposing his army into a square  
 battalion found he had 231 over and above;  
 but increasing each side with one soldier  
 he wanted 44 to fill up the square; How  
 many men did his army consist of?  
 $231 + 44 = 275$ , and  $275 - 1 \div 2 = 137$ , then  $137 \times 137$   
 $+ 231 = 19000$  Answer.

$$\begin{array}{r} 231 \\ + 44 \\ \hline 275 \\ \hline 275 \\ \hline 137 \\ 137 \\ \hline 959 \\ + 411 \\ \hline 1370 \end{array}$$
 19000 Ans.



Suppose a lighthouse built upon the top of a  
 rock; the distance between the place of observa-  
 tion and that part of the rock level with the  
 eye, 620 yards; the distance from the top of  
 the rock to the place of observation 846 yards  
 and from the top of the lighthouse 900 yards.  
 The height of the lighthouse is required?





(45)

Continued. October 8<sup>th</sup> 1810.

900  
900  
81000

620  
620  
12400  
3720  
384400  
810000  
475600

425600 (652.38  
36  
125656  
1302 ) 3100  
2604  
15043 49600  
39129  
1048100  
1049744

846  
846  
3046  
3384  
6768  
331 3.16 (575.60  
23

104 ) 813  
740  
1145 7416  
5725  
11506 69100  
69036  
115120 6400

652.38  
575.60  
76.78 Ans.

A and B have between them a number of Guin  
which are to be so divided that the sum of  
their squares may be 208, and the difference  
of these squares 80; supposing A to be the greater  
number, how many has he more than B?

$208 - 80 \div 2 = 64$  the square of B's, and  $208 - 64 = 144$  the square of A's; therefore  $\sqrt{144} - \sqrt{64} = 4$  Ans.

208  
208  
64

64  
64

208  
208  
64

144  
144

144  
144

12  
12  
4 Ans.

(460)

M. Questions. Continued. Oct. 9<sup>th</sup> 1810.

A and B have 50 Guineas between them which are to be so divided, as that the sum of the squares of the two numbers shall be 1300; How many had each supposing A to have the greater number?

$50 \times 50 - 1300 = 1200$ ; Then  $\sqrt{1300 - 1200} = 10$  difference

Now  $50 \div 2 + 10 \div 2 = 30 = A$ . And  $50 \div 2 - 10 \div 2 = 20 = B$ .

$$\begin{array}{r} 50 \\ 50 \\ \hline 2500 \\ 1300 \\ \hline 1200 \end{array}$$

$$\begin{array}{r} 1300 \\ 1200 \quad (10) \\ \hline 100 \\ 2000 \end{array}$$

$$\begin{array}{r} 3)50 \\ 25 \\ \hline 25 \text{ Ans.} \end{array}$$

$$\begin{array}{r} \sqrt{20} \\ 4 \\ \hline 20 \text{ B's.} \end{array}$$

A number of Guineas are to be divided between A and B in such a manner that A may have 50 more than B and that the sum of the squares of the respective shares may 12500; What number had each?

$12500 - 50 \times 50 = 10000$ , and  $\sqrt{12500 + 10000} = 150$   
= sum of their shares. Then,  $150 \div 2 + 50 \div 2 = 100$  A's;

$150 \div 2 - 50 \div 2 = 50$  B's. Ans.

$$\begin{array}{r} 50 \\ 50 \\ \hline 2500 \\ 12500 \\ \hline 10000 \end{array}$$

$$\begin{array}{r} 3)12500 \\ 9000 \quad (150) \\ \hline 35000 \end{array}$$

$$\begin{array}{r} 10000 \\ 12500 \\ \hline 22500 \end{array}$$

$$\begin{array}{r} 2)100 \\ 50 \\ \hline 50 \text{ B's Share} \end{array}$$

$$\begin{array}{r} 2)50 \\ 25 \\ \hline 25 \text{ A's share} \end{array}$$

Let the sum of the squares of two numbers be 3161 and the square of their Half sum 1560,25; Required those numbers?

$3161 - 1560,25 \times 2 = 40,5$   $40,5 \div 2 = 20,25$ , and  
 $\sqrt{20,25} = 4,5 = \frac{1}{2}$  difference and  $\sqrt{1560,25} = 39,5 = \frac{1}{2}$  sum;  
then,  $39,5 + 4,5 = 44$  the greater, and  $39,5 - 4,5 = 35$  the less.

$$\begin{array}{r} 1560,25 \\ 3161,50 \\ \hline 3161,50 \\ 240,25 \\ \hline 39,5 \end{array}$$

$$\begin{array}{r} 2)40,5 \\ 20,25 \quad (4,5) \\ \hline 40,5 \end{array}$$

$$\begin{array}{r} 39,5 \\ 69,5 \\ \hline 3161 \end{array}$$

44 the greater. 35 the less.

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Continued. Oct. 9<sup>th</sup> 1810.

Suppose the battering ram of Tophet weighed 60000 lb; that it was moved at the rate of 4 feet in one second and that this was sufficient to demolish the walls of Jerusalem; with what velocity must a Cannon ball which weighed 24 lb. be moved to do the same execution?

The velocity of the ram being 44, and the weight of the ball 42, compounded, will make a fraction  $\frac{24}{42} = \frac{4}{7}$ , and  $\frac{4}{7} \times 60000 = 34285 \frac{5}{7}$  feet in a second.

$$\begin{array}{r} 60000 \\ \frac{4}{7} \\ \hline 34285 \frac{5}{7} \end{array}$$

A Body weighing 30 lb. is impelled by such a force as to send it 20 rods in a second; with what velocity would a body weighing 12 lb. move if it were impelled by the same force?

$$\frac{30 \times 20}{12} = 50 \text{ rods.}$$

$$\begin{array}{r} 300 \\ 12 \overline{) 600} \\ \underline{120} \\ 480 \\ \underline{480} \\ 0 \end{array} \text{ 50 Rods in a second, Answer.}$$

### Of Gravity.

Supposing a body to weigh 400 lb. at 2000 miles above the earth's surface; what would it weigh at the surface, estimating the earth's semidiameter at 4000 miles?

From the center to the given height being 1 semidiameter, multiply the square of 4 by the weight and the product will be the

$$1,5 \times 1,5 \times 400 = 900 \text{ lb. ans}$$

$$\begin{array}{r} 1,5 \\ \underline{1,5} \\ 2,25 \\ \underline{2,25} \\ 900,00 \end{array}$$

M. Questions Continued. Oct. 10<sup>th</sup> 1810.

If a Body weigh 900 lb. at the Surface of the Earth; what will it weigh at 2000 miles above the surface?

$1\frac{1}{3} = 1,5$  and  $900 \div 1,5 \times 1,5 = 400$  lb. Ans.

$$\begin{array}{r} 1,5 \\ 1,5 \\ \hline 4,5 \\ 1,5 \overline{) 900,00} \end{array} \quad \begin{array}{l} 400 \text{ lb. Ans.} \\ \hline 900 \\ \hline 00 \end{array}$$

A certain Body on the Surface of the Earth weighs 180 lb. how high must it be carried to weigh 20 lb.  $\sqrt{180 \div 20} = 3$ , Answer, 3 Semidiameters from the Earth's Centre, that is 8000 above its surface.

How high must a Ball be raised to lose half its weight? to 1:40000 X 40000 :: 2:32000000, and  $\sqrt{32000000} = 5656,85$  miles, and  $5656,85 - 4000 = 1656,85$  miles, say

$$\begin{array}{r} 1:16000000::2 \\ \hline 32000000 \end{array} \quad \begin{array}{r} 5656,85 \\ 25 \\ \hline 106 \overline{) 636} \\ 1125 \overline{) 6400} \\ 11306 \overline{) 74500} \\ 113128 \overline{) 966400} \\ 1131365 \overline{) 6137600} \\ \hline 55656825 \end{array}$$

$$\begin{array}{r} 4000 \\ 4000 \\ \hline 16000000 \\ \hline 5656,85 \\ 4000 \\ \hline 1656,85 \end{array}$$

If the attraction of the Moon raise a Tide <sup>on Earth</sup> 5 feet high; what will be the height of a Tide, raised by the Earth on the surface of the Moon under similar circumstances?

The attraction of one of those Bodies to the other's surface is directly as its quantity of matter and inversely as its diameter; therefore,  $2182 \times 2182 \times 2182 \times 494 : 5 :: 8000 \times 8000 \times 8000 \times 4000 : 199,5$  feet ans.

M. Questions Continued. Oct. 15<sup>th</sup> 1810.

2182  
2182  
 4364  
 14456  
 2182  
4364  
 4761124  
2182  
 9522248  
 38088992  
4961124  
 9522248  
10388972568  
 494

8000  
8000  
 64000000  
8000  
 512000000000  
400  
 20480000000000

41555090272  
 93298953172  
41555090272

feet.

5132053648 592:5::20480000000000  
 513,205,364,8592 ) 1024000000000000 (199,5  
 55132053648592  
51079463514080  
 46188482837328  
48909806764520  
 46188482837328  
27213239301920  
 25660268242960  
21552971058960

Of the fall of Bodies.

Heavy bodies near the surface of the Earth fall one foot the first Quarter of a second, three feet in the second Quarter; five feet in the third, and seven feet in the fourth Quarter; that is 16 feet in the first second. The velocities, acquired by Bodies in falling are in proportion to the squares of the Times in which they fall. For instance let go three bullets together, stop the first at one second and it will have fallen 16 feet. Stop the next at the end of the second second and it will have fallen (2x2=4) 4 times 16, or 64 feet, and stop the last at the end of the third second and the distance fallen will be (3x3=9) 9 times 16 or 144 feet, and so on. Or which is the same, the space fallen through h in feet is always equal to the square of the Time in  $\frac{1}{4}$  of a second. Or by multiplying 16 feet by so many odd numbers, beginning at unity as there are seconds in the given time; by one for the first second 3 for the second by 5 for the third and so on these several products will give the spaces fallen

M. Questions Continued. Oct. 18<sup>th</sup> 1810.

through, in each of the several seconds, and their sum will be the whole distance fallen.

The Velocity given to find the space fallen through.

Rule. The square root of the feet in the space fallen through will ever be equal to 1/8 of the velocity acquired at the end of the fall; Therefore,

1. Divide the velocity by 8 and the square of the Quotient will be the distance fallen through to acquire that velocity.

Suppose the velocity of a cannon ball to be about 1/8 of a mile or 660 feet per second; from what height must a body fall to acquire the same velocity per second?

660 ÷ 8 = 82,5 and 82,5 × 82,5 = 6806 1/4 feet, = 1 3/4 miles, Ans.

Handwritten long division: 660 divided by 8 equals 82,5 with a remainder of 0. Below it, 82,5 multiplied by 82,5 equals 6806,25.

The Time given to find the space fallen through

Rule. The square root of the feet in the space fallen through, will ever be equal to 4 times the number of seconds the body has been falling, therefore,

2. Multiply the Time by 4 and the square of the product will be the space fallen through in the given time. How many feet will a body fall in 5 seconds?

5 × 4 = 20 and 20 × 20 = 400 feet, Ans.

A Bullet is dropped from the top of a building, and found to reach the ground in 1 3/4 of a second; Required its height?

1 3/4 × 4 = 7 and 7 × 7 = 49 feet, Ans. Or 1 3/4 = 7/4

Handwritten calculations for the bullet problem: 7/4 × 4 = 7, 7 × 7 = 49 feet, Ans. Also shows 7/4 = 1 3/4.

(51)  
Continued. Oct. 19<sup>th</sup> 1810.

What is the difference between the depth of 2 wells into each of which should a stone be dropped at the same instant one would reach the bottom in 5 seconds and the other in 3?

$$5 \times 4 = 20 \text{ and } 20 \times 20 = 400 \text{ feet.}$$

$$3 \times 4 = 12 \text{ and } 12 \times 12 = 144 \text{ feet.}$$

Answer 56 feet.      Ans. 256 feet.

Ascending Bodies are are retarded in the same ratio that Descending Bodies are accelerated; therefore If a ball discharged from a gun returned to the Earth in 12 seconds; How high did it ascend? The ball being half of the Time or 6 seconds in its ascent, therefore,

$$6 \times 4 = 24 \text{ and } 24 \times 24 = 576 \text{ feet, ans.}$$

$$\begin{array}{r} 64 \\ 24 \\ \hline 96 \\ 432 \\ \hline 576 \text{ feet, Ans.} \end{array}$$

The Velocity per second given to find the Time.  
Rule 1. Four times the number of seconds in which a body has been falling is equal to  $\frac{3}{4}$  of the velocity, in feet per second acquired at the end of the fall; therefore,  
2. Divide the given velocity by 3 and 1 fourth part of the Quotient will be the answer.

How long must a bullet be falling to acquire the velocity of 160 feet per second?

$$6) 160 \div 3 = 20 \text{ and } 20 \div 4 = 5 \text{ seconds, ans.}$$

$$\begin{array}{r} 4) 20 \\ \hline 5 \text{ seconds, Ans.} \end{array}$$

How high must a cannon ball be raised to descend with a velocity of 5,224,49 feet per second?

$$As 16: 4000 \times 4000 :: 5,224,49: 49000000, \text{ and } 49000000 = 7000 \text{ Therefore, } 7000 - 4000 = 3000 \text{ miles, answer.}$$

$$16: 16000000 :: 5,224,49$$

$$\begin{array}{r} 96000000 \\ 16000000 \\ \hline 522449 \times 2589996 \\ \hline 4702049 \\ \hline 4702049 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 4000 \\ 16000000 \\ \hline 19000000 \\ \hline 49 \\ \hline 000000 \end{array}$$

No. Questions Continued. Oct. 19<sup>th</sup> 1810.

The space through which a body has fallen given to find the Time it has been falling.

Rules. 1. Times the number of seconds in which the Body has been falling will ever be equal to the square root of of the space in feet through which it has fallen; therefore, 2. Divide the square root of the space fallen through by 4 and the Quotient will be the time in which it was falling.

In how many seconds will a bullet fall through a space of 10125 feet?

$\sqrt{10125} = 100,6$ , and  $100,6 \div 4 = 25,15$  seconds, = 25<sup>s</sup> 9<sup>ms</sup> Ans.

10125 (100,6  
20001 2500  
2000) 1012500

4) 100,6  
25,15 = 25<sup>s</sup> 9<sup>ms</sup>

5) 25  
20  
5

60 9) 60  
54  
6  
69 3) 69  
63  
6

In what Time would a musket ball, dropped from the top of a Steeple 484 feet high come to the ground?

$\sqrt{484} = 22$  and  $22 \div 4 = 5\frac{1}{2}$  Seconds; Ans.

484 (22 seconds, Ans.  
4  
42) 484

How many feet will a body fall in 5 seconds?

$5 \times 4 = 20$  and  $20 \times 20 = 400$  feet, Ans.

A Bullet is dropped from the top of a building, and found to reach the ground in  $1\frac{3}{4}$  of a second; Required its height?  $1\frac{3}{4} \times 4 = 7$  and  $7 \times 7 = 49$  feet, Ans. Or  $1\frac{3}{4} = 1,75$

49 feet, Ans.  $1,75$   
7,00  
49 feet, Ans.  $1,75$   
7,00  
49 feet, Ans.



Continued. Oct. 20<sup>th</sup> 1810

To find the velocity per second with which a heavy body will begin to descend at any distance from the Earth's surface.

Rule. As the square of the Earth's Semidiameter is to 16 feet: so is the square of any other distance from the Earth's center inversely to the velocity with which it begins to descend per second.

With what velocity per second will an iron ball begin to descend, if raised 3000 miles above the Earth's surface?

As  $4000 \times 4000 : 16 :: 4000 + 3000 \times 4000 + 3000 : 5,22449$

$$\begin{array}{r} 4000 \\ \times 4000 \\ \hline 16000000 \end{array} \qquad \begin{array}{r} 4000 \\ \times 3000 \\ \hline 12000000 \end{array} \qquad \begin{array}{r} 3000 \\ \times 3000 \\ \hline 9000000 \end{array} \qquad \begin{array}{r} 4000 \\ \times 3000 \\ \hline 12000000 \end{array} \qquad \begin{array}{r} 3000 \\ \times 3000 \\ \hline 9000000 \end{array} \qquad \begin{array}{r} 4000 \\ \times 3000 \\ \hline 12000000 \end{array}$$

- feet per sec.

Miles.      Feet.      Miles.

$$16000000 : 16 :: 49000000$$

$$\begin{array}{r} 96000000 \\ 16000000 \\ \hline 49000000 \end{array}$$

$49000000 \overline{) 556000000} (5,22449 \text{ Ans.}$

$$\begin{array}{r} 245000000 \\ \underline{110000000} \\ 98000000 \\ \underline{120000000} \\ 98000000 \\ \underline{220000000} \\ 196000000 \\ \underline{740000000} \\ 790000000 \\ \underline{440000000} \\ 441000000 \\ \underline{441000000} \\ 0 \end{array}$$

How high must a Ball be raised above the Earth's surface, to begin to descend with a velocity of 5,22449 feet per second?

As  $16 : 4000 \times 4000 :: 5,22449 : 49000000$ , and  $49000000 = 7000$ . Therefore,  $7000 - 4000 = 3000$  miles, answer.

$$16 : 16000000 :: 5,22449$$

$$\begin{array}{r} 96000000 \\ 16000000 \\ \hline 49000000 \end{array} \qquad \begin{array}{r} 4000 \\ \times 4000 \\ \hline 16000000 \end{array}$$

7000

$$5,22449 \overline{) 5569796} (49000000$$

$$\begin{array}{r} 4702049 \\ \underline{4702049} \\ 0 \end{array} \qquad \begin{array}{r} 49000000 \\ \times 7000 \\ \hline 00100000 \end{array}$$

(54)  
 M. Questions Continued. October 23<sup>d</sup> 1810.

To find the mean velocity of a falling Body.

Rule. Divide the space fallen through by the number of seconds it was falling, and the Quotient will be the mean velocity.

A musket-Ball dropped from the top of a steeple 484 feet high in  $5\frac{1}{2}$  seconds; required its mean velocity.

$484 \div 5,5 = 88$  feet per Second, Ans.

$$\begin{array}{r} 5,5 \overline{) 484} \phantom{0} \\ \underline{440} \phantom{0} \\ 440 \\ \underline{440} \\ 0 \end{array}$$

To find the velocity acquired by a falling Body per Second (or by a stream of water, having the perpendicular descent given) at the end of any given period of Time.

Rule. 1. The velocity acquired at the end of any Period is equal to twice the mean velocity with which it passed during that Period.

Or 2. Multiply the perpendicular space fallen through by 64, and the square root of the product is the velocity required.

If a ball fall through the space of 484 feet in  $5\frac{1}{2}$  seconds; with what velocity will it strike?

By the first part of the rule

$484 \div 5,5 = 88$ , and  $88 \times 2 = 176$

By the last part

without the Sixth  
 $\sqrt{484 \times 64} = 176$  Ans.

$$\begin{array}{r} 5,5 \overline{) 4840} \phantom{0} \\ \underline{440} \phantom{0} \\ 440 \\ \underline{440} \\ 0 \end{array} \quad \begin{array}{r} 88 \\ 176 \text{ Ans.} \end{array}$$

$$\begin{array}{r} 484 \\ \times 64 \\ \hline 1936 \\ 2904 \\ \hline 30976 \end{array} \quad \begin{array}{r} 176 \text{ Ans.} \end{array}$$

$$\begin{array}{r} 27 \overline{) 2076} \\ \underline{1818} \\ 2586 \\ \underline{2076} \\ 0 \end{array}$$

(55)  
Continued. Oct. 24<sup>th</sup> 1810.

There is a sluice (or flume) one end of which is 2 1/2 feet lower than the other; what is the velocity of the stream per second?  $2,5 \times 64 = 160$  and  $\sqrt{160} = 12,649$  feet, Ans.

2,5  
64  
1500  
1600

160 (12,649 feet Ans.)

22) 440  
440  
0

246) 3100  
492  
2524  
576  
0

25289) 330409  
50578  
25289  
330409  
0

The velocity with which a falling body strikes given to find the space fallen through.  
Rule. Divide the square of the velocity by 64, and the Quotient will be the height required.

If a ball strike the ground with a velocity of 56 feet per second from what height did it fall?

$56 \times 56 \div 64 = 49$  feet, Ans.

56  
56  
3136

64) 3136 (49  
256  
576  
3136  
0

The mean velocity of a fluid or stream is 12,649 feet per second; what is the perpendicular fall of the stream?

$12,649 \times 12,649 \div 64 = 2 1/2$  feet, answer.

2,499956  
1000000 = 2 1/2 nearly

12649  
113841  
50596  
45494  
25298  
12649  
64) 159997201249956  
128  
319  
256  
639  
376  
637  
376  
612  
576  
360  
320  
484

600 seconds therefore  $3600 \times 5600$   
018 miles and 96 feet, for how

M. Questions Continued Oct. 25<sup>th</sup> 1810.

The weight of a body and the space fallen through given to find the force with which it will strike.  
Rule. The momentum or force with which a falling body strikes is equal to its weight multiplied by its velocity therefore find the velocity by Problem 70<sup>th</sup> and multiply it by the weight, which will produce the force required.

If the rammer used for driving the piles of Charlestown Bridge weighed 2 1/2 tons or 4500 lb. and fell through a space of 10 feet, with what force did it strike the pile?

$10 \times 64 = 25,3 = \text{velocity}$  &  $25,3 \times 4500 = 113850 \text{ lb. force}$   

$$\begin{array}{r} 64 \overline{) 25,3} \\ 128 \\ \underline{125} \\ 33 \\ 166 \\ \underline{160} \\ 63 \end{array}$$

$$\begin{array}{r} 4500 \\ \times 25,3 \\ \hline 13500 \\ 22500 \\ \hline 113850 \end{array}$$

The weight and Momentum or striking force given to find the space fallen through.

Rule. Divide the Momentum by the weight and the Quotient will be the velocity, then divide the square of the velocity by 64 and the Quotient will be the space fallen through

If the aforementioned rammer weighed 4500 lb. and struck with a force of 113850 lb. From what height did it fall?  $113850 \div 4500 = 25,3$ , &  $25,3 \times 25,3 \div 64 = 10 \text{ feet}$ , Answer.

$$\begin{array}{r} 4500 \overline{) 113850} \\ 9000 \\ \underline{23850} \\ 22500 \\ \underline{13500} \\ 13500 \end{array}$$

$$\begin{array}{r} 25,3 \\ \times 25,3 \\ \hline 1265 \\ 506 \\ \hline 64 \overline{) 10,09} \\ 64 \\ \underline{369} \\ 309 \end{array}$$

In N. York

(57)  
Continued. Oct. 25<sup>th</sup> 1810

Of Pendulums

The Time of a vibration in the Cycloid is to the Time of a heavy Body's decent through half its length as the circumference of a circle is to the Diameter, that is, as 3,1416 to 1; Therefore as a Body descends freely, by gravity through about 193,5 Inches in the first second, To find the length of a Pendulum, vibrating seconds.

Rule. As 3,1416 x 3,1416 : 1 x 1 :: 193,5 : 19,6 Inches the  $\frac{1}{2}$  length, and 19,6 x 2 = 39,2 Inches, the length.

|            |                  |
|------------|------------------|
| 3,1416     |                  |
| 3,1416     |                  |
| 788,496    |                  |
| 3,1416     |                  |
| 1256,64    |                  |
| 3,1416     |                  |
| 9424,8     |                  |
| 9,86965    | 19,6             |
| 056        | : 1 :: 193,5     |
| 0000000000 | : 0000000000     |
| 9,86965056 | ) 193,5000000000 |
|            | 193,5000000000   |
|            | 9486963056       |
|            | 9480349440       |
|            | 8882685504       |
|            | 597663936        |
|            | 986965056        |
|            | = 19,6           |

To find the length of a pendulum, that will swing any given time.

Rule. Multiply the square of the seconds in any given Time by 39,2 and the Product will be the Length required in Inches.

Required the lengths of several Pendulums, which will swing respectively  $\frac{1}{4}$  seconds,  $\frac{1}{2}$  seconds, minutes and hours?  
 $25 \times 25 \times 39,2 = 2,45$  Inches for  $\frac{1}{4}$  seconds,  $5 \times 5 \times 39,2 = 9,8$  Inches for  $\frac{1}{2}$  seconds,  $1 \times 1 \times 39,2 = 39,2$  Inches for seconds,  $60 \times 60 \times 39,2 =$  the Inches in 2 miles and 120 feet, for Minutes; and 1 hour = 3600 seconds therefore  $3600 \times 3600 \times 39,2 =$  the Inches in 8018 miles and 96 feet, for hours.  
 Ans.

Mr. Questions Continued Oct. 29<sup>th</sup> 1810

What is the Difference between the length of a Pendulum which vibrates Half-seconds and one which swings 3 seconds?

$$\frac{3 \times 3 \times 39,2}{9} - \frac{5 \times 5 \times 39,2}{25} = 28 \frac{7}{12} \text{ feet, ans.}$$

$$\begin{array}{r} 392 \\ 3 \overline{) 1176} \\ \underline{1176} \\ 0 \end{array} \quad \begin{array}{r} 392 \\ 5 \overline{) 1960} \\ \underline{1960} \\ 0 \end{array}$$

$$\begin{array}{r} 11760 \\ 12 \overline{) 141120} \\ \underline{141120} \\ 0 \end{array} \quad \begin{array}{r} 1960 \\ 25 \overline{) 78400} \\ \underline{78400} \\ 0 \end{array}$$

28 <sup>7</sup>/<sub>12</sub> ans.

To find the Time which a Pendulum of any given length will swing.

Rule. Divide the given length by 39,2 and the Quotient will be the square of the time in seconds.

Or, as 6,2696 (the square root of 39,2) is to the square root of the given length; So is 1 second, to the time of oscillation; that is, divide the square root of the given length by 6,2696 and the Quotient will be the time of one vibration of that Pendulum.

How often will a Pendulum of 9,8 Inches vibrate in a second? By the former part of the rule  $9,8 \div 39,2 = 25$  of a second and  $\sqrt{25} = 5$  of a second, the time of one vibration, that is, it vibrates half-seconds or  $60 \div 5 = 120$  times in a minute.

By the latter part.  $\sqrt{9,8} = 3,13$ , and  $\sqrt{39,2} = 6,2696$ , therefore  $3,13 \div 6,2696 = 5$  of a second.

I Observed that while a stone was falling from a Precipice a string (with a Bullet at the end) which measured 25 Inches (to the middle of the Ball) had made 5 vibrations; what was the height of the precipice?

$25 \div 39,2 = 6377$  and  $\sqrt{6377} = 7985$  of a second, the Time of one vibration, and,  $7985 \times 5 = 4$  seconds, nearly, the Time of the stone's descent, then  $4 \times 4 = 16$ , and  $16 \times 16 = 256$  feet, Answer

$$\begin{array}{r} 392 \overline{) 25000} \\ \underline{2332} \\ 16680 \\ \underline{1736} \\ 3040 \\ \underline{2942} \\ 960 \end{array} \quad \begin{array}{r} 6377 \overline{) 7985} \\ \underline{149} \\ 1347 \\ \underline{1388} \\ 5960 \\ \underline{5965} \\ 5 \end{array} \quad \begin{array}{r} 7985 \\ 5 \overline{) 39925} \\ \underline{39925} \\ 0 \end{array}$$

256 feet, ans.

(59)  
Continued. Oct. 30<sup>th</sup> 1810.

To find the true depth of a well by dropping a stone into it also the time of the stone's descent, and of the sound's ascent. Rule. 1. Take a line of any length and by the last Problem find the time from the dropping of the stone till you hear it strike the bottom.

2. Multiply  $73088 (= 16 \times 4 \times 1142; 1142$  feet being the distance, the which sound moves in a second) by the number of seconds till you hear the stone strike the bottom.

3. To this product add  $1304164 (=$  the square of  $1142)$  and from the square root of the sum take  $1142$ .

4. Divide the square of the remainder by  $64 (= 16 \times 4)$  and the quotient will be the depth of the well in feet.

5. Divide the depth by  $1142$  and the quotient will be the time of the sound's ascent, which being taken from the whole time will leave the time of the stone's descent in seconds.

Suppose I drop a stone into a well, and a string with a plummet which measured to the middle of the Ball 25 Inches made 5 vibrations before I heard the stone strike the Bottom; Required the Depth, Time of the stone's descent, and of the sound's ascent?

$25 \div 39,2 = 6377$ , and  $6377 \times 5 = 31885$ , and  $31885 \times 5 = 159425$  seconds to the hearing of it strike, then  $\sqrt{159425 \times 4 + 1304164} - 1142 = 121,53$  and  $121,53 \times 121,53 \div 64 = 230,77$  feet, the depth, and  $230,77 \div 1142 = 2$  of a second, the time of the sound's ascent, and  $4 - 2 = 2$  seconds, the time of the stone's descent.

M. Questions Continued. Oct. 30<sup>th</sup> 1870.

Of the Lever or Steelyard.

It is a principal in Mechanics that the Power is to the weight as the velocity of the weight, to the velocity of the Power. Therefore, to find what weight may be raised or balanced by any given power, say;

As the Distance between the body to be raised or balanced and the Fulcrum or Prop, is to the distance between the Prop and the Point Where the power is applied; So the Power to the weight it will balance.

If a man weighing 160 lbs. rest on the end of a lever 10 feet long; what weight will he balance on the other end, supposing the prop one foot from from the weight?

The distance between the weight and prop being 1 foot the distance from the prop to the Power is 10 - 1 = 9 feet, Therefore

As 1 : 9 :: 160 :: 1440 Ans. 1 : 9 :: 160  
1440 lbs. Ans.

If a weight of 1440 lbs. were to be raised with a lever of 10 and the prop fixed 1 foot from the weight; what Power or weight, applied to the other end of the Lever, would balance it?

As 9 : 1 :: 1440 : 160 lbs. Ans.  
9 : 1 :: 1440  
9 | 1440  
160 lbs. Ans.

If a weight of 1440 lbs. be placed 1 foot from the prop, what distance from the prop must a power of 160 lbs. be applied to balance it?

As 160 : 1440 :: 1 : 9 feet, Ans. 160 : 1440 :: 1  
(60) | 1440  
160

At what distance from a weight of 1440 lbs. must a prop be placed, so as that a power of 160 lbs. applied 9 feet from the prop, may balance it?

As 1440 : 160 : 9 : 1 foot, Ans. 1440 | 1440  
160 1 foot, Ans.



(61)  
Continued. Oct. 20<sup>th</sup> 1810.

In giving directions for making a chaise the length of the shafts between the axle-tree and back-band, being settled at 9 feet, a dispute arose whereabout on the shaft the center should be fixed. The Chaise-maker advised to fix it 30 Inches before the axle-tree; others supposed 20 Inches would be a sufficient Incumbrance for the Horse; Now supposing 2 passengers to weigh 3 Cwt. and the Body of the Chaise  $3\frac{3}{4}$  Cwt. more; what will the beast in both these cases bear, more than his harness?

Weight of the Chaise and Passengers  $3\frac{3}{4}$  Cwt. of 20 lbs. in the lb. } Ans. the  
and 9 feet = 108 Inches. Then, As 108:420::30:116 $\frac{2}{3}$  } Ans. the  
and 9 feet = 108 Inches. Then, As 108:420::20:77 $\frac{1}{3}$  } Ans. the

$$\begin{array}{r} 108:420::30 \\ 108 \overline{) 12600} \quad 116\frac{2}{3} \text{ Ans.} \\ \underline{1080} \\ 180 \\ \underline{180} \\ 0 \end{array}$$

$$\begin{array}{r} 108:420::20 \\ 108 \overline{) 8400} \quad 77\frac{1}{3} \text{ Ans.} \\ \underline{1080} \\ 7320 \\ \underline{7200} \\ 120 \\ \underline{108} \\ 12 \end{array}$$

## Of the Wheel and Axle.

The proportion for the wheel and axle (in which the Power is applied to the circumference of the wheel and the weight is raised by a rope which coils about the axle as the wheel turns round) is As the Diameter of the axle is to the Diameter of the wheel, so is the Power applied to the wheel, to the weight suspended by the axle. A Mechanic would make a windlass in such a manner as that 1 lb. applied to the wheel, should be equal to 10 lb. suspended from the axle; Now, supposing the axle to be 6 Inches diameter; Required the Diameter of the Wheel?  $\frac{60}{1}$  in.  $\frac{60}{1}$  in.

As 10:6::1:60 Inversely the Diameter required

$$\begin{array}{r} 10:6::1 \\ 10 \overline{) 60} \quad 6 \text{ Ans.} \end{array}$$

Suppose the Diameter of the wheel to be 60 Inches required the Diameter of the axle so as 1 lb. on the wheel may balance 10 lb. on the axle?  $\frac{60}{10}$  in.  $\frac{60}{10}$  in.

Inversely, As 1:60::10:6 Diameter required.

$$\begin{array}{r} 1:60::10 \\ 10 \overline{) 60} \quad 6 \text{ Ans.} \end{array}$$

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M. Questions Continued. Oct. 31<sup>st</sup> 1810.

Suppose the Diameter of the axle 6 inches and that of the wheel 60; what Power at the wheel will balance at the Axle? Inversely As  $\frac{6 \text{ in.}}{60 \text{ in.}} :: 60 : 1$   $\frac{6}{60} :: 60$   
 $\frac{6}{60} = \frac{1}{10}$  Ans. 6

Suppose the Diameter of the wheel 60 inches and that of the Axle 6 inches; what weight at the axle will balance 1 lb at the wheel? Inversely, As  $\frac{60 \text{ in.}}{6 \text{ in.}} :: 6 : 10$ , Ans. 6  
 $\frac{60}{6} = 10$  Ans. 6

Of the Screw.

The Power is to the weight which is raised as the distance between two threads of the Screw is to the circumference of a Circle Described by the Power applied at the Lever. Rule. Find the Circumference of the circle Described by the end of the Lever; then as the circumference is to the distance between the spiral threads of the Screw; So is the weight to be raised to the Power which will raise it abating the friction which is not proportional to the Quantity of surface; but to the weight of the Incumbent part; and at a medium  $\frac{1}{3}$  part of the effect of the machine is destroyed by it, sometimes more and sometimes less.

There is a Screw whose threads are an inch asunder & the Lever by which it is turned 30 Inches long and the weight to be raised a ton, or 2240 lb. what Power or force must be applied to the end of the Lever sufficient to turn the Screw - that is, to raise the weight? The Lever being the Semidiameter of the circle the Diameter is 60 Inches; then  $3.1416 \times 30 = 188.496$  inches, the circumference: Therefore, As  $\frac{188.496 \text{ in.}}{1 \text{ in.}} :: 2240 : 11.88$ , Ans.

Continued. Oct. 31<sup>st</sup> 1810.

Let the Lever be 30 Inches, the circumference of which is found to be 188,496 the Threads 1 inch asunder and the Power 11,88 lbs;

Required the weight to be raised? in. in. lbs. lbs. at  
As 1: 188,496 :: 11,88: 2240 nearly

1: 188,496 :: 11,88  
11,88  
1509968  
1509968  
188496  
188496  
229933248

Let the weight be 2240 lbs. the Power 11,88 lbs. and the Lever 30 Inches; Required the distance between the threads?

As 2240: 11,88 :: 188,496: 1 nearly, Ans.

Let the Power be 11,88 lbs. the weight 2240 lbs. and the threads an inch asunder to find the length of the Lever?

As 11,88: 2240 :: 1: 188,5 Then as 355: 113 :: 188,5: 60 inches nearly the diameter and 60 ÷ 2 = 30 inches, Ans.

Suppose one of those Meteors called Fire-balls to move parallel to the Earth's surface and 50 Miles from it at the rate of 20 miles per second; in what time would it move round the Earth?

Suppose the Earth's Diameter 8000 miles, then 8000 + 50 x 2 = 8100 the diameter of the circle described by the Ball Then, as 113: 355 :: 8100: 25446 miles nearly its circumference, and 25446 ÷ 20 = 1272 to Seconds = 2130 3/4 Ans.

8000 50  
100 100  
8100  
113: 355 :: 8100  
35500  
25440  
113) 254460  
226  
284  
612  
262  
305  
4530  
530  
45  
780  
1618  
102  
113

M. Questions. Continued. Oct. 31<sup>st</sup> 1810. c

Sound uninterrupted, moves about 1142 feet in a second; how long then after the firing of a cannon at Newbury port before it will be heard at Ipswich estimating the distance at 10 miles in a right line?

10 miles = 52800 feet, and  $52800 \div 1142 = 46 \frac{134}{571}$  seconds, etc.

|   |  |
|---|--|
| $\begin{array}{r} 1142 \overline{) 52800} \\ \underline{4568} \\ 7122 \\ \underline{6832} \\ 290 \\ \underline{264} \\ 260 \end{array}$ | $\begin{array}{r} 1142 \overline{) 52800} \\ \underline{11420} \\ 41380 \\ \underline{41380} \\ 0 \end{array}$ |
|---|--|

In a thunder storm I observed by my clock that it was 6 seconds between the lightning and the thunder; at what distance was the explosion?

$1142 \times 6 = 6852 \text{ feet} = 1 \frac{13}{140}$

|   |  |
|---|--|
| $\begin{array}{r} 1142 \times 6 \\ \hline 6852 \end{array}$ | $\begin{array}{r} 1142 \overline{) 6852} \\ \underline{2284} \\ 4568 \\ \underline{4568} \\ 0 \end{array}$ |
|---|--|

Tubes may be made of gold weighing not more than at the rate of 165 of a grain per foot; what would be the weight of such a tube, which would extend across the Atlantic, from Boston to London estimating the distance at 3000 miles?  $3000 \times 5280 = 15840000 \text{ feet}$

and  $15840000 \times \frac{165}{100} = 9944 \frac{69}{100}$  grains = 202.6 part.  $\frac{369}{100}$  gr.

Ans. 
$$\begin{array}{r} 5280000 \\ \times 165 \\ \hline 15840000 \end{array}$$

The mean distances of the Planets from the Sun in English miles are as follows; viz. Mercury 36841468. Venus 68891486. The Earth 95143200. Mars 145014148. Jupiter 494990996. Saturn 907956130. and the Moon 240000 from the Earth. Now as a Cannon ball at its first Discharge flies about a Mile in 8 seconds and sound 1142 feet per Second; How long would a Bullet at the above mentioned rate be in passing from the Earth to the Sun, and sound in moving from the Sun to Saturn?

Continued. Nov. 1<sup>st</sup> 1810

$95173000 \times 8'' = 24$  Years, 52 days, 8 hours, 33 minutes, 20 sec.  
 for the passage of the Ball; and  $907956130 \times 5280 =$   
 $= 4794008366400$  feet, and  $4794008366400 \div 1142 =$   
 $\frac{428}{925} \frac{10}{120} \frac{55}{149} \frac{521}{271}$ ; So long would sound be in passing  
 from Sun to Saturn.

Light passes from the Sun to the Earth in about 8 minutes.  
 How long would it be passing from the Sun to Herschel's almi  
 Planet, or the Georgium Sidus, supposing it to be 50000000000  
 miles? As  $95173000 : 8'' :: 50000000000 : 7.0 \frac{1}{17} \frac{1}{2}$ . Answer.

The Diameter of the Sun is 890000 miles. — Mercury's  
 Diameter 3000, Venus's 7924, the Earth's 7970, Mars's 4233, Jupit  
 er's 156446, Saturn's 114172, and the Moon's 2182; what is the  
 comparative magnitude between the Sun and the Earth,  
 and between the Earths and all others?

The Sun =  $890000 \times 890000 \times 890000 \div 7970 \times 7970 \times 7970$   
 $= 1392499,52$  times larger than the Earth. — The Earth =  
 $7970 \times 7970 \times 7970 \div 3000 \times 3000 \times 3000 = 18,75$  larger than  
 Mercury. =  $7970 \times 7970 \times 7970 \div 7924 \times 7924 \times 7924 =$   
 $1,0175$  times larger than Venus. =  $7970 \times 7970 \times 7970 \div$   
 $4233 \times 4233 \times 4233 = 3,28$  times larger than Mars. =  
 $7970 \times 7970 \times 7970 \div 2182 \times 2182 \times 2182 = 48,82$  times larger  
 than the Moon. Jupiter =  $94000 \times 94000 \times 94000 \div 7970 \times$   
 $7970 \times 7970 = 1640,62$  times larger than the Earth. — Saturn  
 $= 114172 \times 114172 \times 114172 \div 7970 \times 7970 \times 7970 = 935,36$   
 times larger than the Earth.

### Spiritous Liquors

The Four following Problems relating to Spiritous Liquors  
 are wrought by alligation.  
 What proportion of rectified Spirits of wine must be mixed  
 with water to make proof spirit; the specific gravity  
 of the rectified spirits being 850, that of proof spirit  
 925, and of water 1000?  $\frac{1000}{925} \frac{75}{75}$  or equal measure

(66) *M. Questions Continued Nov. 1<sup>st</sup> 1870.*

What proportional weight of rectified spirits of wine and water must be mixed, to make proof spirit the specific gravities as before?

Ans.  $\frac{1000}{850} = \frac{20}{17}$  or as 20 to 17.

What is the specific gravity of best French Brandy consisting of 5 parts, measure, of rectified spirits of wine, and 3 parts water?

$$\begin{array}{r} 850 \times 5 = 4250 \\ 1000 \times 3 = 3000 \\ 5 + 3 = 8 \quad \overline{) 7250} \\ \underline{4000} \phantom{00} \\ 3250 \\ \underline{3200} \\ 50 \end{array}$$

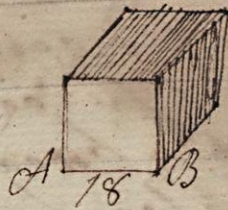
906,25 = Specific gravity.

A Retailer has 50 gallons of Rum, whose specific gravity is 900. How much water must be added, to reduce it to standard proof?  $900 \left\{ \begin{array}{l} 1000 \\ 900 \end{array} \right\} \begin{array}{l} 25 \\ 75 \end{array} \left\} \begin{array}{l} \text{G. Rum} \\ \text{G. Wat.} \end{array} \right. \text{At } 75 : 25 :: 30 : 10 \text{ to be added}$



(67)  
Of Solids. Nov. 5<sup>th</sup> 1810.

Multiply the side by itself and that product by the same side and this last product will be the solid content of the cube.  
Example. The side of a cube A B, being 18 inches or 1 foot and 6 inches to find the content?



1 Foot 6 inches = 1,5 Feet  

$$\begin{array}{r} 1,5 \\ \times 1,5 \\ \hline 2,25 \\ \times 1,5 \\ \hline 3,375 \end{array}$$
  
 Inches operation, the inches are changed into the decimal parts of a foot.

To measure a parallelepipedon.

Definition. A Parallelepipedon is a solid of 3 dimensions by length, breadth, and thickness, as a piece of timber exactly squared whose length is more than the breadth and thickness. The ends are called Bases, which are equal.

Rule. Find the area of the Base, then multiply that by the length and it will give the solid content.

Example. 1. The side of B is 17,5 foot and the length is 9,5 feet to find the solid content?



17,5 = 1 foot 9 inches.  

$$\begin{array}{r} 17,5 \\ \times 17,5 \\ \hline 1225 \\ \times 17,5 \\ \hline 30625 \end{array}$$
 = area of the base.  

$$\begin{array}{r} 30625 \\ \times 9,5 \\ \hline 275625 \\ \times 9,5 \\ \hline 2909375 \end{array}$$
 = Solid Content.

Example 2. A Vessel 3,5 feet each side within, and 5 feet deep to find the content?

$$\begin{array}{r} 3,5 \\ \times 3,5 \\ \hline 12,25 \\ \times 5 \\ \hline 61,25 \end{array}$$
 = the content

of solids. Continued. Nov. 7<sup>th</sup> 1810.

If a piece of timber or any other thing be of an equal bigness through its whole length though there be a difference between the breadth and thickness are multiplied together and that product multiplied by the length this last product will be the solid content.

Examp. 3. A piece of timber being 1 foot and 6 inches or 18 inches broad, 9 inches thick, and 9 feet 6 inches or 114 inches long, to find the content?

$$1 \text{ foot } 6 \text{ inches} = 1,5 \text{ Foot}$$

$$9 \text{ inches} = \frac{75}{100} \text{ Foot}$$

$$\begin{array}{r}
 105 \\
 9 \text{ feet } 6 \text{ inches} \underline{=} 9 \text{ feet} \\
 5625 \\
 10125 \\
 \hline
 106875 = \text{Content}
 \end{array}$$

In this operation the inches are changed into the decimal part of a foot.

To measure a Cylinder.

Definition. A cylinder is a round Body, whose Bases are circles like a round column, or a rolling Stone of a garden.

Rule. The Diameter of the base being given find the area of the end by multiplying the square of the Diameter by .7854 then multiplying the area of the base by the length and that product will be the content of the cylinder.

Example. The Diameter of the Base AC being 1 foot, and 9 inches, and the length BD 12 feet, 6 inches, to find the content?



$$\begin{array}{r}
 12 \\
 2405 = \text{area of Base} \\
 12,5 = \text{length} \\
 \hline
 12025 \\
 24810 \\
 2405 \\
 \hline
 300625 = \text{Content}
 \end{array}$$

$$\begin{array}{r}
 1195 \\
 175 \\
 578 \\
 1225 \\
 175 \\
 3005 \\
 1225 \\
 1580 \\
 1450 \\
 24810 \\
 2405 \\
 27215
 \end{array}$$



(69)  
Continued. Nov. 8<sup>th</sup> 1810.

To find how much a cylindrical or round tree, that is equally thick from end to end, will be worth, when made square.

Rule. Multiply twice the square of its semidiameter by the length then divide the product by 144, and the quotient will be the answer.

If the diameter of a round stick of Timber be 24 inches from end to end and its length 20 feet; how many solid feet will it contain when hewn square; and what will be the content of the slabs which reduce it to a square?

$$\begin{array}{r} 2 \\ 4 \\ \hline 7854 \\ 314820 \\ \hline 628520 \end{array}$$

$$\begin{array}{r} 12 \\ \hline 144 \\ 2880 \quad (40 \\ \hline 144 \overline{) 5760} \\ \underline{4320} \\ 1440 \\ \underline{1440} \\ 0 \end{array}$$

the solid feet of the slabs.

To measure a Prism.

Rule. Prisms of all kinds, whether square, triangular or polygonal, are measured by one general rule viz. Find the superficial content or area at the base (or end) by the proper rule and this multiplied by the length or height of the Prism, will be the solid content.

Examp. The side of a stick of Timber, A B, hewn square, is 10 inches, and the length A C, is 12 feet; to find the content?

Side = 10 inches  
 $\frac{1}{2}$  perp. = 5 inches  
 Area at the end = 25 square inches  
 Length = 12 feet  
 $25 \times 12 = 300$  solid feet

$$\begin{array}{r} 144 \overline{) 3004} \\ \underline{432} \\ 420 \\ \underline{420} \\ 0 \end{array}$$

Artificers, When they set off the corner of a building usually measure 6 feet on one side and 8 on the other then laying a ten feet pole across it makes the corner a true right angle.

# Of solids Continued. Nov. 9<sup>th</sup> 1810. 6

To measure a Pyramid.

Rule. Find the area of the base whether triangular square, polygonal, or circular, by the Rules in superficial measures; then multiply this area by one third of the height, and the product will be the solid content of the Pyramid.

Examp. 1. In a triangular pyramid the height BE being 48 and each side of the base 13; the base being a triangle let the perpendic. height DE be 11; to find the content?



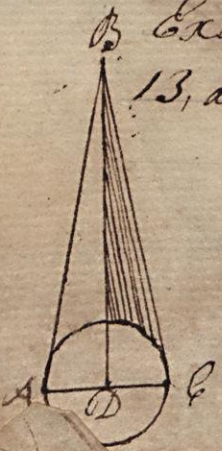
|                           |
|---------------------------|
| 5,5 = Half ED             |
| 13 = Base AC              |
| 165                       |
| 5,5 = Area of the base    |
| 16 = 1/3 of the height EB |
| 4290                      |
| 715                       |
| 1144,0 Content.           |

Examp. 2. In a quadrangular Pyramid, the height BE being 48 and each side of the base 13, to find the content.

|                           |
|---------------------------|
| 13                        |
| 39                        |
| 139 = area of the base.   |
| 16 = 1/3 of the height EB |
| 1014                      |
| 169                       |
| 2704 = Content.           |



Examp. 3. To measure a Cone. The diameter AC being 13, and the height BD 48 to find the content.



|                      |
|----------------------|
| 13                   |
| 63,1                 |
| 63,1                 |
| 169                  |
| 676                  |
| 845                  |
| 1352                 |
| 1811                 |
| 1927,26 = area base. |
| 16 = 1/3 of height   |
| 7763,956             |
| 1527,826             |
| 2257,16 = Content.   |

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Continued, Nov. 9<sup>th</sup> 1810.

Note. the superficial content of all Pyramids is found by taking the sum of the several areas, which compose them. That of a cone by multiplying the circumference of the base into half the line joining the vertex and any point in that circumference, and adding the area of the base to the product.

To measure the frustum of a Pyramid.

Examp. 1. In the frustum of a square Pyramid the side of the greater base  $AD = 15$ , the side of the less  $BC = 6$ , and the height  $EF = 40$ , to find the content.

|   |  |  |
|---|--|--|
| $\begin{array}{r} 15 = AD \\ 6 = BC \\ \hline \text{Prod} = 90 \\ \text{Add } 27 \\ \hline 117 \\ \times 40 \\ \hline 4680 = \text{Content.} \end{array}$ | $\begin{array}{r} 15 \\ 6 \\ \hline 9 = \text{Difference} \\ 9 \\ \hline 361 \\ 27 \\ \hline = \frac{1}{3} \text{ of the square.} \end{array}$ |  |
|---|--|--|



If there be a tapering square stick of timber, take the girth of it in the middle; square  $\frac{1}{4}$  of the girth then say as 144 (inches) is to that product; so is the length taken in feet, to the content in feet.

Examp. 2. In the frustum of a triangular pyramid the side of the greater base  $AC = 15$ , as before the side of the less  $BD = 6$ , and the height  $EF = 40$ , to find the content.

|   |   |  |
|---|---|--|
| $\begin{array}{r} 15 = AC \\ 6 = BD \\ \hline 9 = \text{Diff. of the sides} \\ 9 \\ \hline 361 = \text{square of diff.} \\ 27 \\ \hline = \frac{1}{3} \text{ of the square.} \end{array}$ | $\begin{array}{r} 15 \\ 6 \\ \hline 225 \\ 90 \\ \hline 315 \\ 117 \\ \hline 432 \\ 351 \\ \hline 583 \\ 40 \\ \hline 208640 = \text{Content.} \end{array}$ | <p>Multipliers.</p> <p>Mean area.</p> <p>Height.</p> |
|---|---|--|



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# Solids Continued. Nov. 10<sup>th</sup> 1810.

To measure the frustrum of a cone.

The former cone being cut off in the middle, the greater diameter A B is 13 the less B D 6 1/2 and height E F 24, to find the content of the frustrum.

A B = 13 inches  
B D = 6 1/2 inches

6 1/2  
7 1/2

---

64 5  
Add 145003  
98583  
7854

---

394332  
4929153  
86664  
790081

13  
6 1/2  
6 1/2 = Difference.  
6 1/2  
32 5

---

390  
372 5 = Square of the diff.  
17,083 = 1/3 of square.

144) 1858248 (13973 feet content.

144  
418  
288  
1302  
1296  
1004  
1008

---

568  
432  
136

774270882 = Mean area.  
24 Feet = Length.

309309  
154854  
1858248 = Content.

To measure a Sphere or Globe.

Rule. Multiply the cube of the diameter by 5236 and the Product will be the solid content.

Or multiply the Circumference by the Diameter which will give the superficial content, then multiply the surface by 1/6 of the diameter, and it will give the solidity.

Or multiply the cube of the diameter by 11, and the product divided by 21, will give the solidity.

Examp. The diameter A B of a Globe is 4,5; to find the solid content.

45  
45  
2025  
180  
2025  
10125  
8100  
91125  
15236

---

2346750  
2735325  
182250  
4295625  
5913050



(43)  
Continued. Nov. 12<sup>th</sup> 1810. 6

To measure the solidity of a frustrum or Segment of a Globe.

Rule. To three times the square of the semidiameter of the Base, add the square of the height; then multiply that sum by the height and the product by  $\frac{5236}{1728}$ , you will have the solid content.

Examp. The height BD being 9 inches and the diameter of the Base AC 24 inches. to find the content.

|                          |           |                  |
|--------------------------|-----------|------------------|
| 12 = Semidiam.           | 4617      |                  |
|                          | 5236      |                  |
| 12 = Square              | 144       |                  |
| $\times 3$               | 432       |                  |
| 9 = Square of the height | 81        |                  |
| $\times 5236$            | 4617      |                  |
| 23085                    | 2417,4612 | = Solid content. |

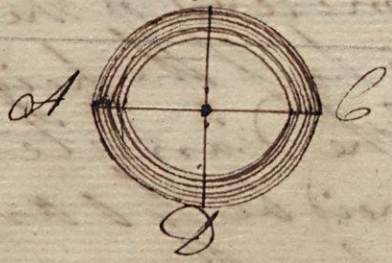


To measure a Spheroid.

Rule. Multiply the square of the diameter of the greatest Circle viz the diameter of the middle (DB in the figure) by the length AC and that product by  $\frac{5236}{1728}$ , and you will have the Solidity.

Examp. The diameter BD being 20 and the length AC 50 to find the content.

|                |           |  |
|----------------|-----------|--|
| 20             | 12000     |  |
|                | 5236      |  |
| $\times 50$    | 60000     |  |
| 316000         | 3160000   |  |
| 240000         | 2400000   |  |
| 600000         | 6000000   |  |
| 6283,2000 ans. | 6283,2000 |  |



To measure the segment of a spheroid.  
Rule. To four times the square of the middle diameter add the square of the base diameter, then multiply that sum by  $\frac{854}{1728}$ , and that product by one sixth of the altitude and it will give the solidity. If the base-diameter of the end-frustum of a

Solids Continued Nov. 13<sup>th</sup> 1810.

The diameter be 30, diameter at the middle of the height 30, and the height 20 inches; Required the solidity?

$30 \times 30 \times 4 + 96 \times 36 \times .7854 \times 3.3 = 12817.728$  Ans. No.  
 $20 \div 6 = 3.3$

To measure a parabolic Conoid.

Rule. As a Parabolic Conoid is half of its circumscribing cylinder, of the same base and altitude; multiply the area of the base by half the height for the solidity.

If the Diameter of the base of a parabolic Conoid be 40 inches, and its height 42; what is the solidity?  $40 \times 40 \times .7854 \times 21 = 26394.4$  Ans.

To measure the lower Frustrum of a Parabolic Conoid.

Rule. Multiply the sum of the squares of the diameters of the bases by .654, and that product by half the height for the solidity.

If the diameters of a frustrum of a parabolic Conoid be 40 and 30 inches and its height 20 inches; Required its solidity?  $40 \times 40 + 30 \times 30 \times .7854 \times 10 = 19635$  Ans.

To measure a parabolic Spindle.  
Rule. This Solid being eight fifteenths of its least circumscribing cylinder multiply the area of its middle or greatest diameter by  $\frac{8}{15}$  of its perpendicular length and it will give its solidity.

(43)  
Continued. Nov. 13<sup>th</sup> 1810.

If the Diameter at the middle of a parabolic Spindle be 20 inches, and its length 60; Required the solidity.  
 $20 \times 20 \times 75 \div 4 = 7500$  ( $= 60 \times 8 \div 15$ )  $10053 \frac{1}{2}$  Ans.

To measure the middle zone or middle Frustrum of a parabolic spindle.

Rule. To the sum and half the sum of the squares of the two diameters add  $\frac{3}{10}$  of the difference of their squares which multiply by a third of the length, and the product will be the Solidity.

If the middle and end diameters of the middle frustrum of a parabolic spindle be 40 and 30 inches, and its length 60; what is the Solidity.  
 $40 \times 40 = 1600$        $1600 + 900 = 2500$  the Diff of the squares  
 $30 \times 30 = 900$        $900 \times 3 = 2700 = \frac{3}{10}$  of ditto, then  
Sum = 2500       $2500 + 1250 + 2700 \times 20 = 49200$   
Half Sum = 1250      Ans.

To measure a Cylindrical or Prismatic.  
Rule. The same as for the frustrum of a pyramid or cone.

To measure a Solid Ring.  
Rule. measure the internal diameter of the ring and its girth or circumference then multiply the girth by 3,1831, and the product will be the Diameter of the wire, which add to the internal diameter; multiply this sum by 3,1416 and the product will be the length of a cylinder equal to the Ring of the same base. Then the area of the section of the Ring multiplied by the length of the said cylinder will give the Solidity of the Ring.

If an Iron ring be 12 inches in girth and its internal diameter be 20 inches what is its Solidity?  
 $3,1831 \times 12 = 3,81972$  Ring diameter.  $20 \times 3,81972 = 76,3944$  the length of a cylinder equal to the Ring, and  $3,81972 \times 3,81972 \times 76,3944 = 110,786$  Solidity

Solids

To measure the Solidity of any irregular body, whose dimensions cannot be taken.

78  
 79  
 80  
 81  
 82  
 83  
 84  
 85  
 86  
 87  
 88  
 89  
 90  
 91  
 92  
 93  
 94  
 95  
 96  
 97  
 98  
 99  
 100

Take any regular vessel either square or round and put the irregular body into it; Pour as much water into the vessel as will exactly cover the body and measure the dry part from the Top of the vessel to the water; - Then take the <sup>out.</sup> body and measure again from the Top of the vessel to the water and subtract the first measure from the second and the difference is the fall of the water; Then if the vessel be square multiply the side by itself and that product by the fall of the water and you will have the content of the body; but if you have a long square multiply the length by the breadth and that product by the fall of the water; - Or lastly if it be a round vessel multiply the square of the diameter by  $\frac{7854}{10000}$  and that product by the fall of the water and you will have the Content.

|   |  |   |
|---|--|---|
| <p>Exampr. 1. A Body being put into a vessel 18 inches square, by 3 on, taking it out the water sunk 9 Inches; Required the Content of the Body?</p> <p>18 Inch. = 1,5 foot.<br/>                 9 Inch. = .75 foot.<br/> <math>1,5 \times 1,5 \times 75 = 1,6875</math><br/>                 foot content. 10</p> | <p>Exampr. 2. A Body put into a cistern 4 feet square, by 3 on, taking it out the water fell 6 inch; Required the Content of the Body?</p> <p><math>4 \times 3 \times .5 = 6</math> feet,<br/>                 Content. 20</p> | <p>Exampr. 3. A Body being put into a round Tub, whose diameter was 1,5 foot on taking out the Body the water fell 1,5 foot; what is the Content of the Body?</p> <p><math>1,5 \times 1,5 \times 7854 \times 1,5 = 2,65</math> feet, Content.</p> |
|---|--|---|

Decorative flourishes and scribbles at the bottom of the page.



# 77 Of Cask Gauging.

Among the many different canons, drawn from Stereome-  
for gauging casks the following is as exact as any.

Take the dimensions of the Cask in inches, viz. the diameter at  
bung and head and length of the Cask; Subtract the head diameter  
from the bung-diameter, and note the difference.

If the staves of the Cask be much curved or bulging between the  
bung and head, multiply the difference by, 7; If not quite so  
curved, by, 6.5; if they bulge yet less, by, 6; and if they are almost  
or quite straight, by, 5.5, and add the product to the head diameter; the sum  
will be a mean diameter by which the cask is reduced to a cylinder.  
Square the mean diameter, thus found, then multiply the  
length; divide the product by 359 for ale or beer-gallons, and by  
294 for wine-gallons.

By the sliding Rule.

On D is 18,94, the gauge-point for ale or Beer Gallons  
marked thus AG, and 17,44, the gauge-point for wine Gallons  
marked thus WG; set the gauge-point to the length of the Cask on C, and aga-  
the mean diameter or D you will have you will have the answer  
all or wine gallons accordingly as which gauge-point you  
make use of.

By the Scale

Take the extent from the gauge-point to the mean diameter  
set one foot of the dividers in the length and turning them  
twice over they will point out the content.

Required the Content of a Cask in wine and Ale  
gallons, whose bung diameter is 35 inches, Head-diam  
27 inches and length 45 inches?

|                    |      |    |         |     |          |
|--------------------|------|----|---------|-----|----------|
| Bung Diameter = 35 | 35   | 35 | 1062,96 | 115 |          |
| Head Diameter = 27 | 27   | 35 | 1956    | 115 | 531380   |
| Diff. = 8          | 8    | 35 | 652     | 115 | 425104   |
| 7th = 4            | 4    | 35 | 976     | 115 | 35977824 |
| 5th = 6            | 6    | 35 | 1062    | 115 | 274824   |
| Mean Diam = 27,6   | 27,6 | 35 | 1062,96 | 115 | 159      |

# Gauging. Continued. Nov. 14<sup>th</sup> 1810.

1 Round Mash-Tub is 42 Inches diameter at the Top within and 36 inches at the bottom and the perpendicular height 48 Inches; Required the content in beer and wine gallons.

2 This being the lower frustum of a cone to the product of the diameters add one third of the square of their difference; multiply this sum by the length, and it will give the solidity in such parts as the dimensions are taken in. If they be taken in inches divide by 359 for beer and 294 for wine gallons.

$$42 \times 36 + \frac{42 - 36 \times 42 - 36}{3} \times 48 \div \begin{cases} 359 = 203 \frac{3}{4} \text{ Ale Gallons} \\ 294 = 248 \frac{3}{4} \text{ Wine Gallons} \end{cases}$$

3 Let the Diff. of diameters of this Tub be 6 inches, the height 48 inches, and the content 203  $\frac{3}{4}$  gallons to find the diameters.

4 Multiply the content if beer measure by 359; if wine measure by 294 and divide the product by the length; from the quotient subtract  $\frac{1}{3}$  of the square of the diff. of the diameters; to this remainder add the square of  $\frac{1}{2}$  the difference of diameters and extract the square root of the sum; from the square subtract  $\frac{1}{2}$  the diff. of the diameters, and it will give the least diameter to great exactness, to which add the difference of the diameters, and the sum is the greatest diameter.

$$\sqrt{\frac{203,75 \times 359}{48} - \frac{6 \times 6}{3} + 3 \times 3} - 3 = 36, \text{ and } 36 + 6 = 42. \text{ The diameters are 36 and 42.}$$

The content of any vessel, in gallons, &c. may be found: Measure the inside of the vessel according to the rule of the figures and find the content in cubic inches, then,

|           |  |   |  |
|-----------|--|---|--|
| Divide by | $\begin{array}{r} 1728 \\ 242 \\ 231 \\ 250,4 \end{array}$ | and the Quotient will be the content in | $\begin{cases} \text{Cubic Feet.} \\ \text{Ale or beer gal.} \\ \text{Wine Gallons.} \\ \text{Bushels.} \end{cases}$ |
|-----------|--|---|--|

Continued. Nov. 16<sup>th</sup> 1810.

To ullage a cask, lying on one side by the Gau-  
-Rod when the Bung Diameter and the content ones  
both are greater or less than the Table on the Rod is  
made for.

Rule. As the bung diameter of the cask, to be measured: is to  
the bung diameter that the Table is made for: so are the <sup>two</sup>  
Inches of the cask: to a fourth number, which find in the Table  
on the Rod and note the number of gallons answering to it.  
Then as the content of the cask that the Table is made for:  
is to the content of the cask to be measured: so is the number  
of gallons answering to the aforesaid fourth number:  
to the number of gallons your cask wants of being full.

To find a Ship's Burthen Or to Gauge a ship.

There is such diversity in the forms of ships that no general  
Rule can be applied to answer all varieties; however the fol-  
-lowing Rules are practiced.

Rule. 1. Multiply the breadth at the Main beam, half the  
breadth and length together: divide the product by 94 and  
the Quotient is the Tons.

Rule. 2. Divide the continued product of the length bread-  
and depth in feet by 100, for ships of war, and 95 for Merchant  
Ships, in which nothing is allowed for guns, &c, and the  
Quotient is the Tons.

Rule. 3. Take the length from the stern post to the upper  
part of the stem; subtract two thirds of the breadth from  
that length: multiply the remainder by the by the  
whole breadth, and that product by half the bread-  
in feet and divide by 100 for war, and 94 for Merch-  
-Gonnage.

Rule. 4. The weight of a ship's burthen is half the  
of water she will hold.  
What is the tonnage of  
breadth 31 feet and

Ship Gauging Continued. Nov. 16<sup>th</sup> 1810. &

By Rule 1. st.

Breadth 15,5  
Breadth 31

155  
465  
460,5

Length, 97  
33635  
43245

94) 4600 8,5 (495,43 Tons. Merchant

376  
907  
1446  
548  
470  
755  
752  
330  
282  
48

By Rule 2 d.

Length 97  
Breadth 31

97  
5007  
15035  
15035  
3007

95) 4660 8,5 (490,61 Tons. Merchant

380  
860  
855  
555  
570  
150  
95  
55

for Ships  
of war.

-ant.

By Rule 2 d.

Length = 97

Subt.  $\frac{2}{3}$  of Breadth = 20,66

Mult by the breadth 76,33  
31

2269,9

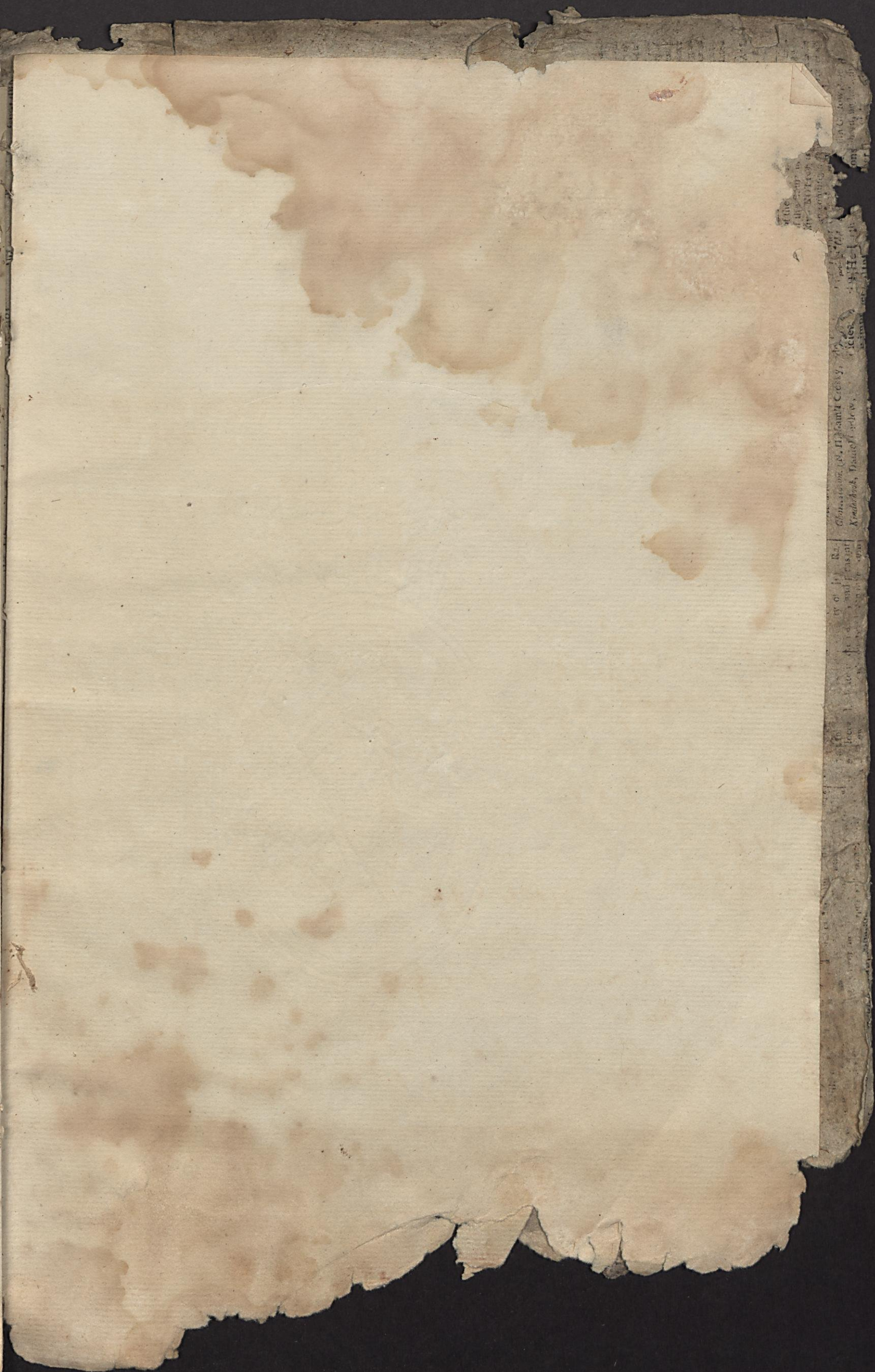
Mult by the breadth 15,5

16831,15  
336623

94) 52176,565 (555,069 Tons. Merchant.

The Proportions of the Ark were as follows, viz.

Length of Keel } 300  
Breadth By Aline-ship-Beam. 50 } Its Burthen as a Man of War  
Depth in Hold. } 30 } 4500 Tons.  
Elect. } } 4736 80 Tons.



21

B  
C  
D

9

L

M

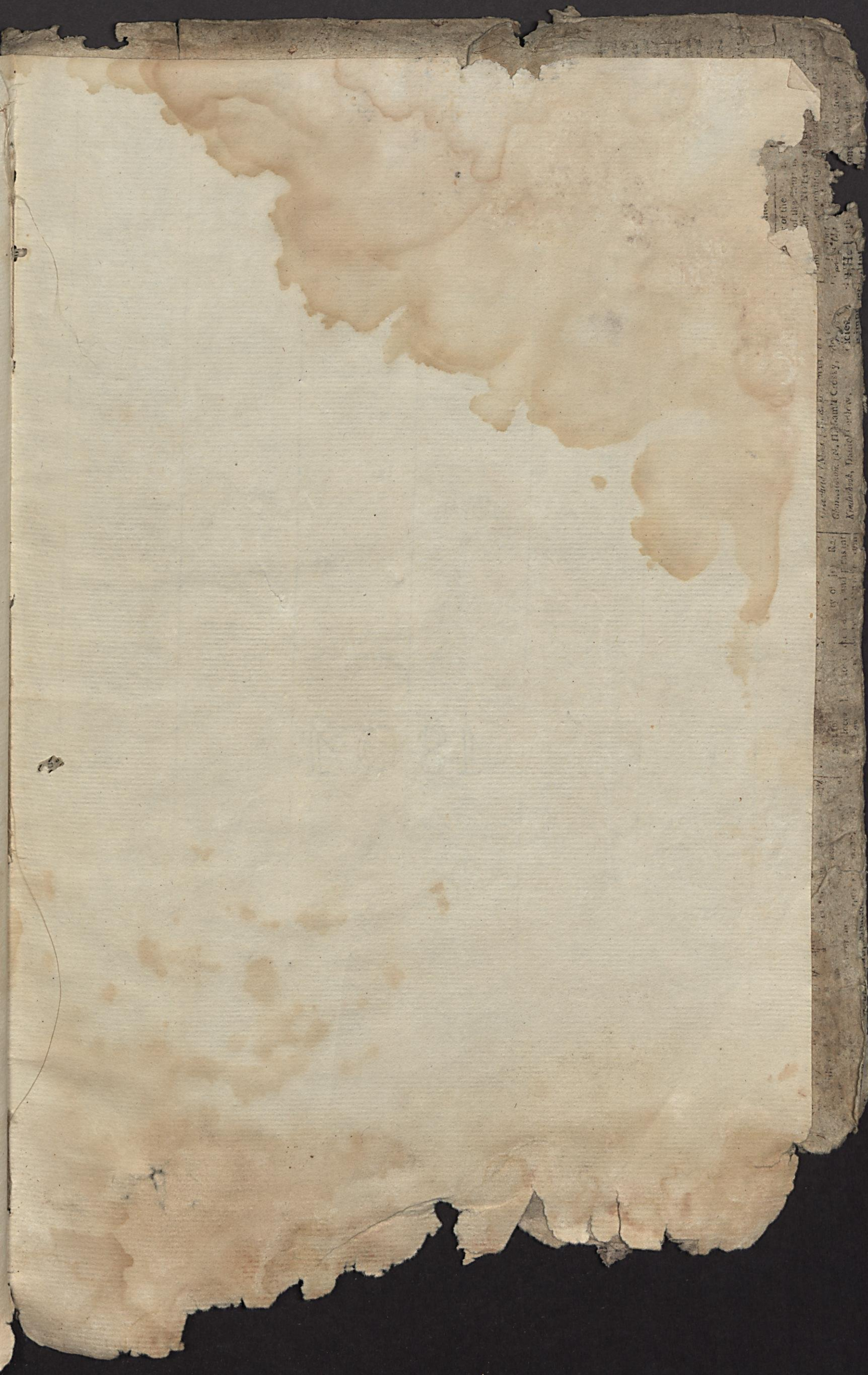
9

L

B

D

*[Faint, illegible handwriting at the bottom of the page]*



204 39 53  
 1465096  
 1836  
 1290  
 1200  
 204 39 2000  
 2264 7 4000 382  
 612  
 1680  
 630  
 280  
 298

63  
 504  
 203 3/4  
 815 ) 312000 382  
 2445  
 6750  
 18520  
 2300  
 1630  
 670  
 3134

2000  
 39000  
 312000  
 382  
 382  
 762

3086  
 1146  
 7459 24  
 48

815  
 163  
 103 ) 1540 822  
 1304  
 360  
 326  
 540  
 626

359 ) 700 43 5 2 29510  
 359  
 3414  
 3233  
 1795  
 385  
 359  
 262

12 ) 382  
 31 10

204 39 800 20  
 204 39 2000 158 12 13 3  
 1080 34  
 1020  
 600 104  
 206 28  
 192 205 59x9.7





